

Sense of Number

Expanded Visual Calculation Policy

Mental Strategies Policy

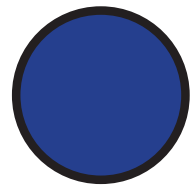
Hawkesley Church Primary Academy
July 2019

Graphic Design by Dave Godfrey
Compiled by the Sense of Number Maths Team

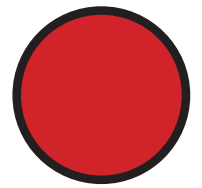
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'A picture is worth 1000 words!' www.senseofnumber.co.uk





Guide to using a



Visual Calculation Policy

The Full Sense of Number Visual Calculation Policy Package provides a comprehensive visual representation of a school's Calculation Policy.

- 1: CPVCP** **Concrete and Pictorial VCP** - The foundation of the policy, featuring key models and images to help children gain deep understanding of the abstract procedures.
- 2: WSVCP** **Written Strategies progression from jottings to formal written methods from Y1 to Y6.**
- 3: MSVCP** **Mental Strategies progression across KS1 and KS2 for all four operations.**
- 4: ECPD** **Editable Calculation Policy Document** - a comprehensive written explanation of a school's calculation policy, featuring thumbnails of the posters from the three documents above.

Typical uses:

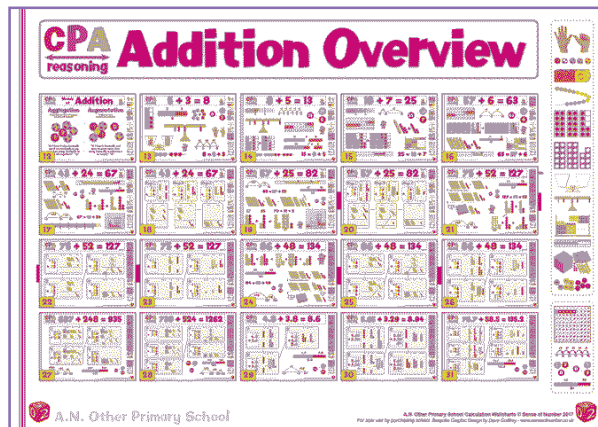
- Classroom:** The posters are printed out (e.g. A4) and the appropriate slides are displayed for continual reference or on a working wall. Posters are used on the interactive whiteboard.
- Reference:** The summary overviews are printed out and inserted in the teacher's planning folder.
- Parents:** The posters are used to communicate to parents the methods being used within school.
- Website:** Screen grabs of slides from the VCP are inserted on a schools' maths webpages.
(PLEASE NOTE: the VCP should not be placed on school website for copyright reasons.)
A secure PDF copy of the Editable Calculation Policy may be placed on the school website.



Expanded Visual Calculation Policy

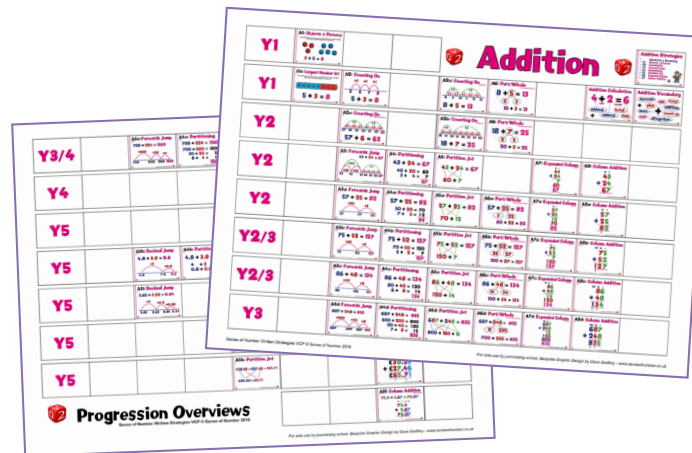
The Expanded Visual Calculation Policy helps children and teaching staff achieve mastery of all aspects of calculation. It contains the following three documents:

Concrete & Pictorial VCP



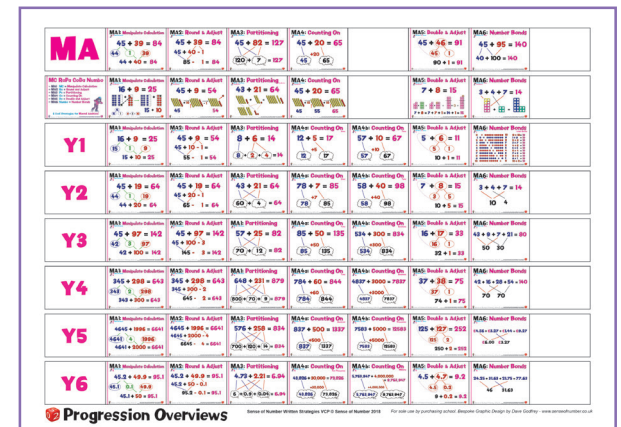
84 A3 wallcharts showing the range of models and images that help children to understand and master calculation strategies.

Written Strategies VCP

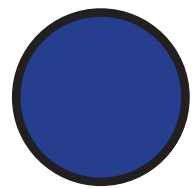


271 A4 posters showing the progression of written strategies (from Y1 to Y6) for all 4 operations in line with the National Curriculum.

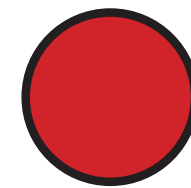
Mental Strategies VCP



214 A4 posters showing the progression of mental strategies (from Y1 to Y6) for all 4 operations in line with the National Curriculum.



Poster Guide



Expanded Visual Calc. Policy

Code	Section	Concrete & Pictorial (84 A3 Wallcharts)		Written VCP (271 A4 Posters)		Mental VCP (215 A4 Posters)	
		Number of Wallcharts	Wallchart Numbers	No. of Posters	Poster Numbers	No. of Posters	Poster Numbers
	Policy Introduction Slides	4	1-4	4	1-4	4	1-4
	Introductory Posters	3	5-7	9	5-13		
	Operation Overviews	4	8-11	13	14-26	8	5-12
C	Counting Policy			15	27-41		
A	Addition	20	12-31	54	42-103		
MA	Mental Addition					55	13-67
S	Subtraction	27	32-58	48	104-169		
MS	Mental Subtraction					63	68-130
M	Multiplication	11	59-69	39	170-209		
MM	Mental Multiplication					46	131-176
D	Division	15	70-84	55	210-264		
MD	Mental Division					38	177-215
	Multiplication Tables			11	265-275		
	Alternative layouts (Column & Number Lines)			29	276-306		



MC RaPa CoDa Numbo

14 **MA1** **MC** = **Manipulate Calculation**

22 **MA2** **Ra** = **Round and Adjust**

30 **MA3** **Pa** = **Partitioning**

38 **MA4** **Co** = **Counting On**

52 **MA5** **Da** = **Double and Adjust**

60 **MA6** **Numbo** = **Number Bonds**



6 Cool Strategies for Mental Addition!



MA	MA1: Manipulate Calculation $45 + 39 = 84$ $44 + 40 = 84$	MA2: Round & Adjust $45 + 39 = 84$ $45 + 40 - 1 = 84$	MA3: Partitioning $45 + 82 = 127$ $120 + 7 = 127$	MA4: Counting On $45 + 20 = 65$	MA5: Double & Adjust $45 + 46 = 91$ $90 + 1 = 91$	MA6: Number Bonds $45 + 95 = 140$ $40 + 100 = 140$

MC RaPa CoDa Numbo MA1 MC = Manipulate Calculation MA2 Ra = Round and Adjust MA3 Pa = Partitioning MA4 Co = Counting On MA5 Da = Double and Adjust MA6 Numbo = Number Bonds 6 Cool Strategies for Mental Addition!	MA1: Manipulate Calculation $16 + 9 = 25$ $15 + 10 = 25$	MA2: Round & Adjust $45 + 9 = 54$ $45 + 10 - 1 = 54$	MA3: Partitioning $43 + 21 = 64$ $40 + 20 + 4 = 64$	MA4: Counting On $45 + 20 = 65$ $45 \rightarrow 55 \rightarrow 65$	MA5: Double & Adjust $7 + 8 = 15$ $7 + 8 = 7 + 7 + 1 = 14 + 1 = 15$	MA6: Number Bonds $3 + 4 + 7 = 14$

Y1	MA1: Manipulate Calculation $16 + 9 = 25$ $15 + 10 = 25$	MA2: Round & Adjust $45 + 9 = 54$ $45 + 10 - 1 = 54$	MA3: Partitioning $8 + 6 = 14$ $8 + 2 + 4 = 14$	MA4a: Counting On $12 + 5 = 17$	MA4b: Counting On $57 + 10 = 67$	MA5: Double & Adjust $5 + 6 = 11$ $10 + 1 = 11$	MA6: Number Bonds $0 + 10 = 10$ $1 + 9 = 10$ $2 + 8 = 10$ $3 + 7 = 10$ $4 + 6 = 10$ $5 + 5 = 10$ $6 + 4 = 10$ $7 + 3 = 10$ $8 + 2 = 10$ $9 + 1 = 10$ $10 + 0 = 10$

Y2	MA1: Manipulate Calculation $45 + 19 = 64$ $44 + 20 = 64$	MA2: Round & Adjust $45 + 19 = 64$ $45 + 20 - 1 = 64$	MA3: Partitioning $43 + 21 = 64$ $60 + 4 = 64$	MA4a: Counting On $78 + 7 = 85$	MA4b: Counting On $58 + 40 = 98$	MA5: Double & Adjust $7 + 8 = 15$ $14 + 1 = 15$	MA6: Number Bonds $3 + 4 + 7 = 14$ $10 + 4 = 14$

Y3	MA1: Manipulate Calculation $45 + 97 = 142$ $42 + 100 = 142$	MA2: Round & Adjust $45 + 97 = 142$ $45 + 100 - 3 = 142$	MA1: Partitioning $57 + 25 = 82$ $70 + 12 = 82$	MA4a: Counting On $85 + 50 = 135$	MA4b: Counting On $534 + 300 = 834$	MA5: Double & Adjust $16 + 17 = 33$ $32 + 1 = 33$	MA6: Number Bonds $43 + 9 + 7 + 21 = 80$ $50 + 30 = 80$

Y4	MA1: Manipulate Calculation $345 + 298 = 643$ $343 + 300 = 643$	MA2: Round & Adjust $345 + 298 = 643$ $345 + 300 - 2 = 643$	MA1: Partitioning $648 + 231 = 879$ $800 + 70 + 9 = 879$	MA4a: Counting On $784 + 60 = 844$	MA4b: Counting On $4837 + 3000 = 7837$	MA5: Double & Adjust $37 + 38 = 75$ $74 + 1 = 75$	MA6: Number Bonds $42 + 16 + 28 + 54 = 140$ $70 + 70 = 140$

Y5	MA1: Manipulate Calculation $4645 + 1996 = 6641$ $4641 + 2000 = 6641$	MA2: Round & Adjust $4645 + 1996 = 6641$ $4645 + 2000 - 4 = 6641$	MA3: Partitioning $576 + 258 = 834$ $700 + 120 + 14 = 834$	MA4a: Counting On $837 + 500 = 1337$	MA4b: Counting On $7583 + 5000 = 12583$	MA5: Double & Adjust $125 + 127 = 252$ $250 + 2 = 252$	MA6: Number Bonds $£4.56 + £3.27 + £1.44 = £9.27$ $£6.00 + £3.27 = £9.27$

Y6	MA1: Manipulate Calculation $45.2 + 49.9 = 95.1$ $45.1 + 50 = 95.1$	MA2: Round & Adjust $45.2 + 49.9 = 95.1$ $45.2 + 50 - 0.1 = 95.1$	MA3: Partitioning $4.73 + 2.21 = 6.94$ $6 + 0.9 + 0.04 = 6.94$	MA4a: Counting On $43,826 + 30,000 = 73,826$	MA4b: Counting On $5,763,947 + 4,000,000 = 9,763,947$	MA5: Double & Adjust $4.5 + 4.7 = 9.2$ $9 + 0.2 = 9.2$	MA6: Number Bonds $24.25 + 31.63 + 21.75 = 77.63$ $46 + 31.63 = 77.63$

MC RaPa CoOCoB NumFa

69 **MS1** **MC** = Manipulate Calculation

77 **MS2** **Ra** = Round and Adjust

85 **MS3** **Pa** = Partitioning

91 **MS4** **CoO** = Counting On

108 **MS5** **CoB** = Counting Back

123 **MS6** **NumFa** = Number Facts



6 Cool Strategies for Mental Subtraction!



MS

MS1: Manipulate Calculation $84 - 29 = 55$ $85 - 30 = 55$	MA2: Round & Adjust $84 - 29 = 55$ $84 - 30 + 1$ $54 + 1 = 55$	MS3: Partitioning $63 - 35 = 28$ 63 30 28	MS4a: Counting On $61 - 58 = 3$ 58 61	MS4b: Counting On $40 - 28 = 12$ 28 30 40	MS5a: Counting Back $68 - 20 = 48$ 48 68	MS5b: Counting Back $86 - 12 = 74$ 86 76 74	MS6: Number Facts $61 - 41 = 20$ $41 + 20 = 61$
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MC RaPa CoOC CoB NumFa
 = MS1 MC = Manipulate Calculation
 = MS2 Ra = Round and Adjust
 = MS3 Pa = Partitioning
 = MS4 CoO = Counting On
 = MS5 CoB = Counting Back
 = MS6 NumFa = Number Facts

6 Cool Strategies for Mental Subtraction!

MS1: Manipulate Calculation $24 - 9 = 15$ $24 - 9 = 25 - 10$	MA2: Round & Adjust $24 - 9 = 15$ 24 14 15	MS3: Partitioning $63 - 35 = 28$ 28 30 63	MS4a: Counting On $12 - 9 = 3$ 9 12	MS4b: Counting On $40 - 28 = 12$ 28 30 40	MS5a: Counting Back $68 - 20 = 48$ 68 48	MS5b: Counting Back $86 - 12 = 74$ 74 76 86	MS6: Number Facts $61 - 41 = 20$ $41 + 20 = 61$
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Y1

MS1: Manipulate Calculation $24 - 9 = 15$ $25 - 10 = 15$	MA2: Round & Adjust $24 - 9 = 15$ $24 - 10 + 1$ $14 + 1 = 15$	MS3: Partitioning $23 - 8 = 15$ 23 20 15	MS4a: Counting On $12 - 9 = 3$ 9 12		MS5a: Counting Back $15 - 4 = 11$ 11 15		MS6: Number Facts $19 - 9 = 10$ $9 + 10 = 19$
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Y2

MS1: Manipulate Calculation $84 - 29 = 55$ $85 - 30 = 55$	MA2: Round & Adjust $84 - 29 = 55$ $84 - 30 + 1$ $54 + 1 = 55$	MS3: Partitioning $63 - 35 = 28$ 63 30 28	MS4a: Counting On $61 - 58 = 3$ 58 61	MS4b: Counting On $40 - 28 = 12$ 28 30 40	MS5a: Counting Back $68 - 20 = 48$ 48 68	MS5b: Counting Back $86 - 12 = 74$ 86 76 74	MS6: Number Facts $61 - 41 = 20$ $41 + 20 = 61$
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Y3

MS1: Manipulate Calculation $463 - 97 = 366$ $466 - 100 = 366$	MA2: Round & Adjust $463 - 97 = 366$ $463 - 100 + 3$ $363 + 3 = 366$	MS3: Partitioning $123 - 28 = 95$ 123 100 95	MS4a: Counting On $302 - 297 = 5$ 297 302	MS4b: Counting On $61 - 37 = 24$ 37 40 61	MS5a: Counting Back $378 - 50 = 328$ 328 378	MS5b: Counting Back $89 - 34 = 55$ 89 59 55	MS6: Number Facts $123 - 83 = 40$ $83 + 40 = 123$
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Y4

MS1: Manipulate Calculation $876 - 298 = 578$ $878 - 300 = 578$	MA2: Round & Adjust $876 - 298 = 578$ $876 - 300 + 2$ $576 + 2 = 578$	MS3: Partitioning $132 - 58 = 74$ 132 80 74	MS4a: Counting On $1003 - 998 = 5$ 998 1003	MS4b: Counting On $324 - 280 = 44$ 280 300 324	MS5a: Counting Back $768 - 200 = 568$ 568 768	MS5b: Counting Back $578 - 45 = 533$ 578 538 533	MS6: Number Facts $847 - 447 = 400$ $447 + 400 = 847$
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Y5

MS1: Manipulate Calculation $5864 - 2996 = 2868$ $5868 - 3000 = 2868$	MA2: Round & Adjust $5864 - 2996 = 2868$ $5864 - 3000 + 4$ $2864 + 4 = 2868$	MS3: Partitioning $750 - 372 = 378$ 750 400 378	MS4a: Counting On $8.3 - 7.9 = 0.4$ 7.9 8.3	MS4b: Counting On $1204 - 950 = 254$ 950 1000 1204	MS5a: Counting Back $7291 - 2000 = 5291$ 5291 7291	MS5b: Counting Back $8.6 - 4.1 = 4.5$ 8.6 4.6 4.5	MS6: Number Facts $1424 - 724 = 700$ $724 + 700 = 1424$
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Y6

MS1: Manipulate Calculation $46357 - 11999 = 34358$ $46358 - 12000 = 34358$	MA2: Round & Adjust $46357 - 11999 = 34358$ $46357 - 12000 + 1$ $46357 + 1 = 34358$	MS3: Partitioning $€64.30 - €24.50 = €39.80$ $€64.30$ $€40$ $€39.80$	MS4a: Counting On $€12.02 - €11.98 = 4p$ $€11.98$ $€12.02$	MS4b: Counting On $12.4 - 9.8 = 2.6$ 9.8 10 12.4	MS5a: Counting Back $86374 - 20000 = 66374$ 66374 86374	MS5b: Counting Back $€65.87 - €30.24 = €35.63$ $€65.87$ $€35.87$ $€35.63$	MS6: Number Facts $13.2 - 9.2 = 4$ $9.2 + 4 = 13.2$
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Mental Multiplication

132	MM1	Manipulate Calculation
139	MM2	Factorising
146	MM3	Re-ordering
149	MM4	Partitioning
154	MM5	Round & Adjust
158	MM6	Doubling
166	MM7	Doubling Table Facts
170	MM8	Doubling Up
173	MM9	Multiply by ... then Halve
175	MM10	Jump



10 Cool Strategies for Mental Multiplication



MM

MM1: Manipulate Calculation $16 \times 3 = 48$ $(+2) \times 2$ $8 \times 6 = 48$	MM2: Factorising $16 \times 3 = 48$ $(8 \times 2 \times 3)$ $8 \times 6 = 48$	MM3: Re-ordering $(9 \times 2) \times 5 = 90$ $18 \times 5 = 90$ $(9 \times 5) \times 2 = 90$ $45 \times 2 = 90$ $(2 \times 5) \times 9 = 90$ $10 \times 9 = 90$ *	MM4: Partitioning $15 \times 5 = 75$ $50 + 25 = 75$ $(10 \times 5) + (5 \times 5)$	MM5: Round & Adjust $49 \times 3 = 147$ $(50 \times 3) - (1 \times 3)$ $150 - 3 = 147$	MM6: Doubling Double 17 = 34 $20 + 14 = 34$	MM7: Doubling Table Facts $8 \times 6 = 48$ (4×2) $4 \times 6 = 24$ $8 \times 6 = 48$ $\times 2$	MM8: Doubling Up $17 \times 4 = 68$ Double 17 = 34 (17×2) Double 34 = 68 (17×4)
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Mental Multiplication <ul style="list-style-type: none"> MM1 Manipulate Calculation MM2 Factorising MM3 Re-ordering MM4 Partitioning MM5 Round & Adjust MM6 Doubling MM7 Doubling Table Facts MM8 Doubling Up MM9 Multiply by ... then Halve MM10 Jump 10 Cool Strategies for Mental Multiplication	MM1a: Manipulate Calculation $27 \times 3 = 81$ $(+3) \times 3$ $9 \times 9 = 81$	MM2a: Factorising $27 \times 3 = 81$ $(9 \times 3 \times 3)$ $9 \times 9 = 81$	MM3a: Re-ordering $(7 \times 4) \times 5 = 140$ $28 \times 5 = 140$ $(7 \times 5) \times 4 = 140$ $35 \times 4 = 140$ $(4 \times 5) \times 7 = 140$ $20 \times 7 = 140$ *	MM4a: Partitioning $37 \times 4 = 148$ $120 + 28 = 148$ $(30 \times 4) + (7 \times 4)$	MM5a: Round & Adjust $198 \times 4 = 792$ $(200 \times 4) - (2 \times 4)$ $800 - 8 = 792$	MM6a: Doubling Double 37 = 74 $60 + 14 = 74$	MM7a: Doubling Table Facts $12 \times 7 = 84$ (6×2) $6 \times 7 = 42$ $12 \times 7 = 84$ $\times 2$	MM8a: Doubling Up $36 \times 8 = 288$ Double 36 = 72 (36×2) Double 72 = 144 (36×4) Double 144 = 288 (36×8)
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MM1b: Manipulate Calculation $45 \times 14 = 630$ $(\times 2) \times 2$ $90 \times 7 = 630$	MM2b: Factorising $45 \times 14 = 630$ $(45 \times 2 \times 7)$ $90 \times 7 = 630$	MM3b: Re-ordering $(9 \times 8) \times 6 = 432$ $72 \times 6 = 432$ $(9 \times 6) \times 8 = 432$ $54 \times 8 = 432$ * $(8 \times 6) \times 9 = 432$ $48 \times 9 = 432$	MM4b: Partitioning $126 \times 6 = 756$ $600 + 120 + 36 = 756$ $(100 \times 6) + (20 \times 6) + (6 \times 6)$	MM5b: Round & Adjust $3.9 \times 5 = 19.5$ $(4 \times 5) - (0.1 \times 5)$ $20 - 0.5 = 19.5$	MM6b: Doubling Double 78 = 156 $140 + 16 = 156$	MM7b: Doubling Table Facts $16 \times 7 = 112$ (8×2) $8 \times 7 = 56$ $16 \times 7 = 112$ $\times 2$	MM8b: Doubling Up $125 \times 16 = 2000$ Double 125 = 250 (125×2) Double 250 = 500 (125×4) Double 500 = 1000 (125×8) Double 1000 = 2000 (125×16)
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MM1c: Manipulate Calculation $36 \times 25 = 900$ $(+4) \times 4$ $9 \times 100 = 900$	MM2c: Factorising $36 \times 25 = 900$ $(9 \times 4 \times 25)$ $9 \times 100 = 900$		MM4c: Partitioning $4.3 \times 8 = 34.4$ $32 + 2.4 = 34.4$ $(4 \times 8) + (0.3 \times 8)$	MM5c: Round & Adjust $\pounds 5.99 \times 6 = \pounds 35.94$ $(\pounds 6 \times 6) - (1p \times 6)$ $\pounds 36 - 6p = \pounds 35.94$	MM6c: Doubling Double 340 = 680 $600 + 80 = 680$	MM7c: Doubling Table Facts $22 \times 12 = 264$ (11×2) $11 \times 12 = 132$ $22 \times 12 = 264$ $\times 2$	
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MM1d: Manipulate Calculation $32 \times 15 = 480$ $(\times 5) \times 3$ $160 \times 3 = 480$	MM2d: Factorising $32 \times 15 = 480$ $(32 \times 5 \times 3)$ $160 \times 3 = 480$		MM4d: Partitioning $2.16 \times 3 = 6.48$ $6 + 0.3 + 0.18 = 6.48$ $(2 \times 3) + (0.1 \times 3) + (0.06 \times 3)$		MM6d: Doubling Double 480 = 960 $800 + 160 = 960$		
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MM1e: Manipulate Calculation $26 \times 32 = 832$ $(\times 4) \times 4$ $104 \times 8 = 832$	MM2e: Factorising $26 \times 32 = 832$ $(26 \times 4 \times 8)$ $104 \times 8 = 832$				MM6e: Doubling Double 278 = 556 $400 + 140 + 16 = 556$		
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MM1f: Manipulate Calculation $52 \times 24 = 1248$ $(\times 4) \times 3$ $208 \times 6 = 1248$	MM2f: Factorising $52 \times 24 = 1248$ $(52 \times 4 \times 6)$ $208 \times 6 = 1248$				MM6f: Doubling Double 768 = 1536 $1400 + 120 + 16 = 1536$	MM9: Mult by 5 then Halve $86 \times 5 = 430$ $86 \times 10 = 860$ $860 \div 2 = 430$	MM10: Jump! $\times 100$ 3400 $\times 10$ 340 34
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MM6g: Doubling Double 3.7 = 7.4 $6 + 1.4 = 7.4$	MM9a: Mult by 5 then Halve $56 \times 25 = 1400$ $56 \times 100 = 5600$ $5600 \div 2 = 2800$ $2800 \div 2 = 1400$	MM10a: Jump! $\times 1000$ 63400 $\times 100$ 6340 $\times 10$ 634 63.4
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Progression Overviews

Sense of Number Written Strategies VCP © Sense of Number 2018




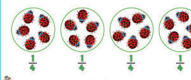

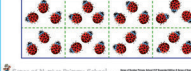
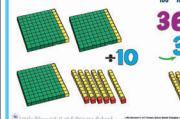
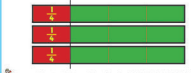
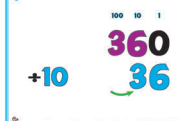

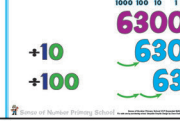

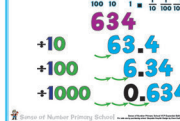


Mental Division

- 178 **MD1** Manipulate Calculation
- 185 **MD2** Divide by 100 then Double
- 187 **MD3** Halving
- 194 **MD4** Halve and Halve Again
- 198 **MD5** Division as a Fraction
- 205 **MD6** Find the Hunk
- 211 **MD7** Jump



7 Cool Strategies for Mental Division!



<h1>MD</h1>	MD1: Manipulate Calculation $140 \div 20$ $\begin{array}{l} +10 \\ +10 \end{array}$ $14 \div 2 = 7$	MD2: Divide by 100 then Double $800 \div 50 = 16$ $800 \div 100 = 8$ $8 \times 2 = 16$	MD3: Halving Half of 12 is equivalent to $12 \div 2$  $\frac{1}{2}$ of 12 = $12 \div 2$	MD4: Halve & Halve Again $84 \div 4 = 21$ Half of 84 = 42 ($84 \div 2$) Half of 42 = 21 ($42 \div 2$)	MD5: Division as Fraction $\frac{1}{4}$ of 20 = $20 \div 4 = 5$ 	MD6: Find the Hunk! $72 \div 4 = 18$ $40 + 32 = 72$ $10 + 8 = 18$	MD7: Jump (+10) 	
Mental Division MD1 Manipulate Calculation MD2 Divide by 100 then Double MD3 Halving MD4 Halve and Halve Again MD5 Division as a Fraction MD6 Find the Hunk! MD7 Jump 7 Cool Strategies for Mental Division!	MD1a: Manipulate Calculation $84 \div 12$ $42 \div 6 = 7$ $21 \div 3 = 7$	MD2a: Divide by 100 then Double twice $800 \div 25 = 32$ $800 \div 100 = 8$ $8 \times 2 = 16$ $16 \times 2 = 32$	MD3a: Halving Half of 26 $10 + 3 = 13$	MD4a: Halve & Halve Again $128 \div 4 = 32$ Half of 128 = 64 ($128 \div 2$) Half of 64 = 32 ($64 \div 2$)	MD5a: Division as Fraction $\frac{1}{8}$ of 24 = $24 \div 8 = 3$ 	MD6a: Find the Hunk! $65 \div 4 = 16r1$ $40 + 25 = 65$ $10 + 6r1 = 16r1$	MD7a: Jump (+10) 	
	MD1b: Manipulate Calculation $1200 \div 400$ $\begin{array}{l} +100 \\ +100 \end{array}$ $12 \div 4 = 3$		MD3b: Halving Half of 58 $25 + 4 = 29$	MD4b: Halve, Halve, Halve $360 \div 8 = 45$ Half of 360 = 180 ($360 \div 2$) Half of 180 = 90 ($180 \div 2$) Half of 90 = 45 ($90 \div 2$)	MD5b: Division as Fraction $\frac{1}{4}$ of 3 = $3 \div 4 = \frac{3}{4}$ 	MD6b: Find the Hunk! $136 \div 4 = 34$ $120 + 16 = 136$ $30 + 4 = 34$	MD7a: Jump (+10) 	
	MD1c: Manipulate Calculation $162 \div 18$ $\begin{array}{l} +2 \\ +2 \end{array}$ $81 \div 9 = 9$		MD3c: Halving Half of 92 $40 + 6 = 46$ Half of 92 $45 + 1 = 46$	MD4c: Halve, Halve, Halve $5000 \div 8 = 625$ Half of 5000 = 2500 ($5000 \div 2$) Half of 2500 = 1250 ($2500 \div 2$) Half of 1250 = 625 ($1250 \div 2$)	MD5c: Division as Fraction $\frac{1}{4}$ of 9 = $9 \div 4 = 2\frac{1}{4}$ 	MD6c: Find the Hunk! $394 \div 6 = 65r4$ $360 + 34 = 394$ $60 + 5r4 = 65r4$	MD7b: Jump (+10/100) 	
	MD1d: Manipulate Calculation $18 \div 1.5$ $\begin{array}{l} \times 2 \\ \times 2 \end{array}$ $36 \div 3 = 12$		MD3d: Halving Half of 326 $160 + 3 = 163$ Half of 326 $150 + 10 + 3 = 163$		MD5d: Division as Fraction $\frac{1}{5}$ of 17 = $17 \div 5 = 3\frac{2}{5}$ 	MD6d: Find the Hunk! $536 \div 4 = 134$ $400 + 120 + 16 = 536$ $100 + 30 + 4 = 134$	MD7c: Jump (+10/100/1000) 	
	MD1e: Manipulate Calculation $9.3 \div 0.3$ $\begin{array}{l} \times 10 \\ \times 10 \end{array}$ $93 \div 3 = 31$		MD3e: Halving Half of 5.84 $2.5 + 0.4 + 0.02 = 2.92$		MD5e: Division as Fraction $\frac{1}{8}$ of 19 = $19 \div 8 = 2\frac{3}{8}$ 	MD6e: Find the Hunk! $18 \div 1.5 = 12$ $15 + 3 = 18$ $10 + 2 = 12$		
	MD1f: Manipulate Calculation $6.25 \div 0.25$ $\begin{array}{l} \times 4 \\ \times 4 \end{array}$ $25 \div 1 = 25$		MD3f: Halving Half of 34.72 = 17.36 $15 + 2 + 0.35 + 0.01$ Half of 34.72 $10 + 7 + 0.3 + 0.6$		MD5f: Division as Fraction $\frac{1}{12}$ of 9 = $9 \div 12 = \frac{3}{4}$ 			



Progression Overviews

Sense of Number Written Strategies VCP © Sense of Number 2018



MC RaPa CoDa Numbo

14 **MA1** **MC** = **Manipulate Calculation**

22 **MA2** **Ra** = **Round and Adjust**

30 **MA3** **Pa** = **Partitioning**

38 **MA4** **Co** = **Counting On**

52 **MA5** **Da** = **Double and Adjust**

60 **MA6** **Numbo** = **Number Bonds**



6 Cool Strategies for Mental Addition!

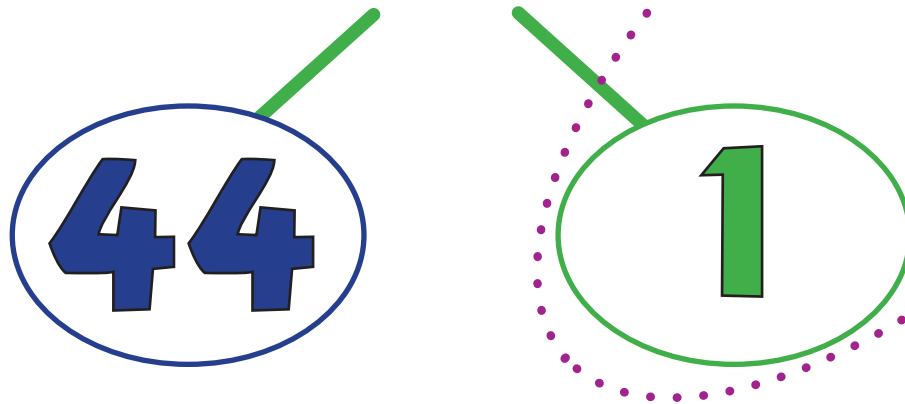


MA1: Manipulate Calculation



MC RaPa CoDa Numbo

$$45 + 39 = 84$$



$$44 + 40 = 84$$

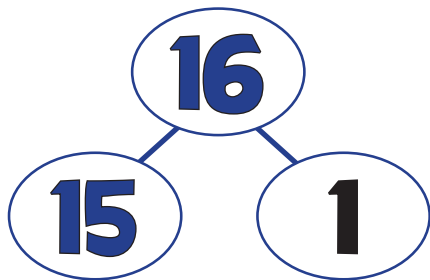
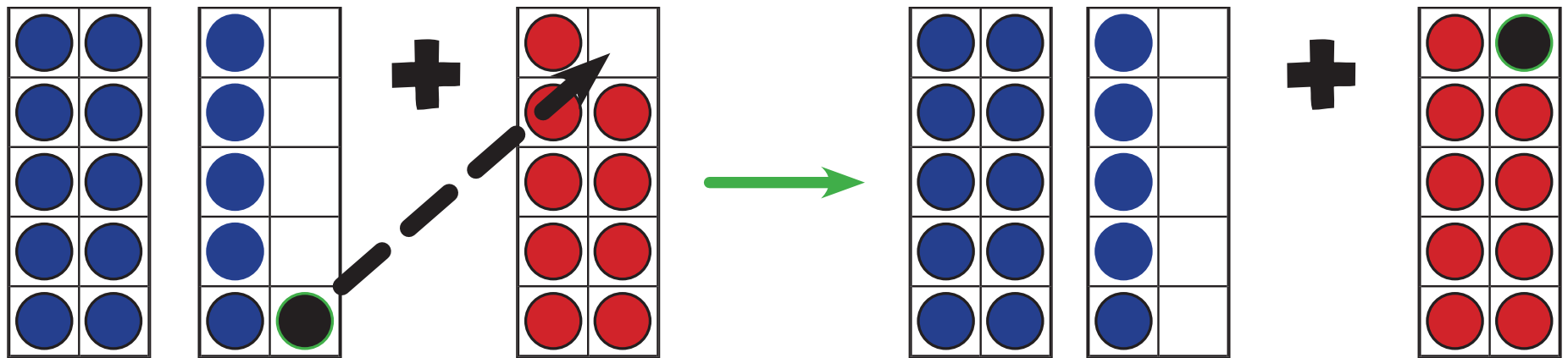


MA1: Manipulate Calculation



MC RaPa CoDa Numbo
Visualisation

$$16 + 9 = 25$$



$$9 + 1 = 10$$

$$15 + 10$$



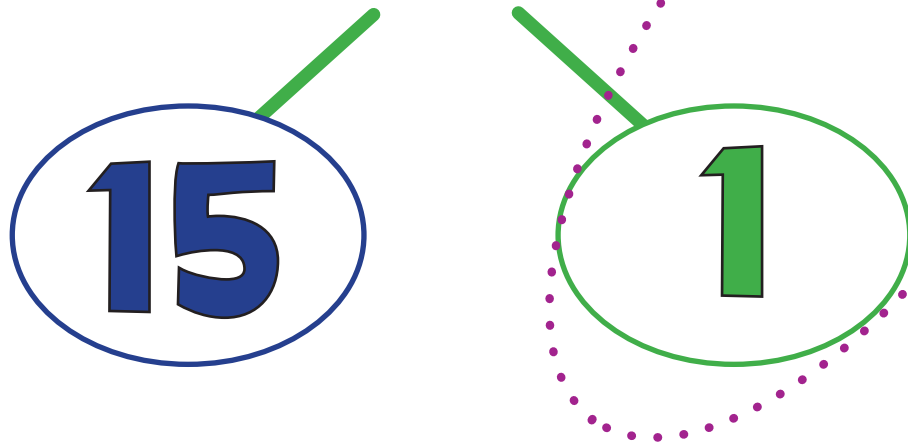
MA1: Manipulate Calculation



MC RaPa CoDa Numbo

1

$$16 + 9 = 25$$



$$15 + 10 = 25$$



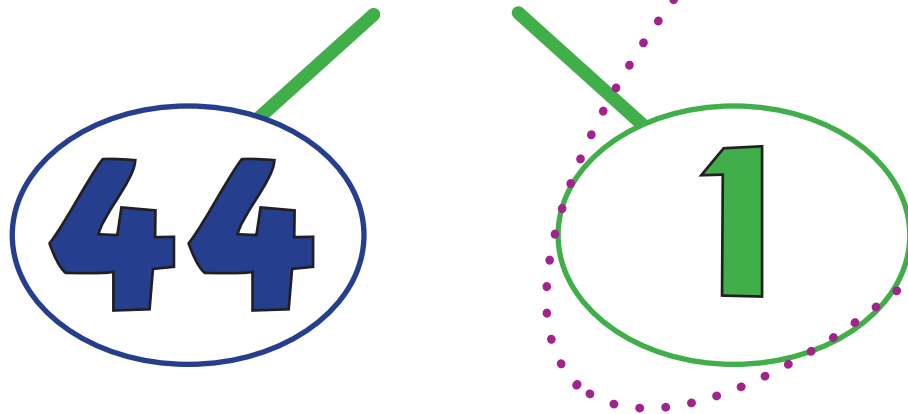
MA1: Manipulate Calculation



MC RaPa CoDa Numbo

2

$$45 + 19 = 64$$



$$44 + 20 = 64$$



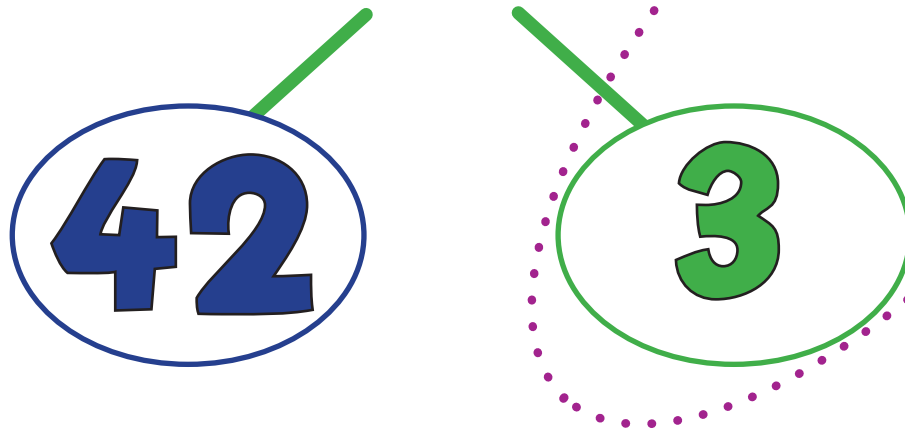
MA1: Manipulate Calculation



MC RaPa CoDa Numbo

3

$$45 + 97 = 142$$



$$42 + 100 = 142$$



MA1: Manipulate Calculation



MC RaPa CoDa Numbo

4

$$345 + 298 = 643$$

$$343$$

$$2$$

$$343 + 300 = 643$$



MA1: Manipulate Calculation



MC RaPa CoDa Numbo

5

$$4645 + 1996 = 6641$$

4641

4

$$4641 + 2000 = 6641$$



MA1: Manipulate Calculation



MC RaPa CoDa Numbo

6

$$45.2 + 49.9 = 95.1$$

$$45.1$$

$$0.1$$

$$45.1 + 50 = 95.1$$



MA2: Round & Adjust



MC RaPa CoDa Numbo

$$45 + 39 = 84$$

$$45 + 40 - 1$$

$$85 - 1 = 84$$

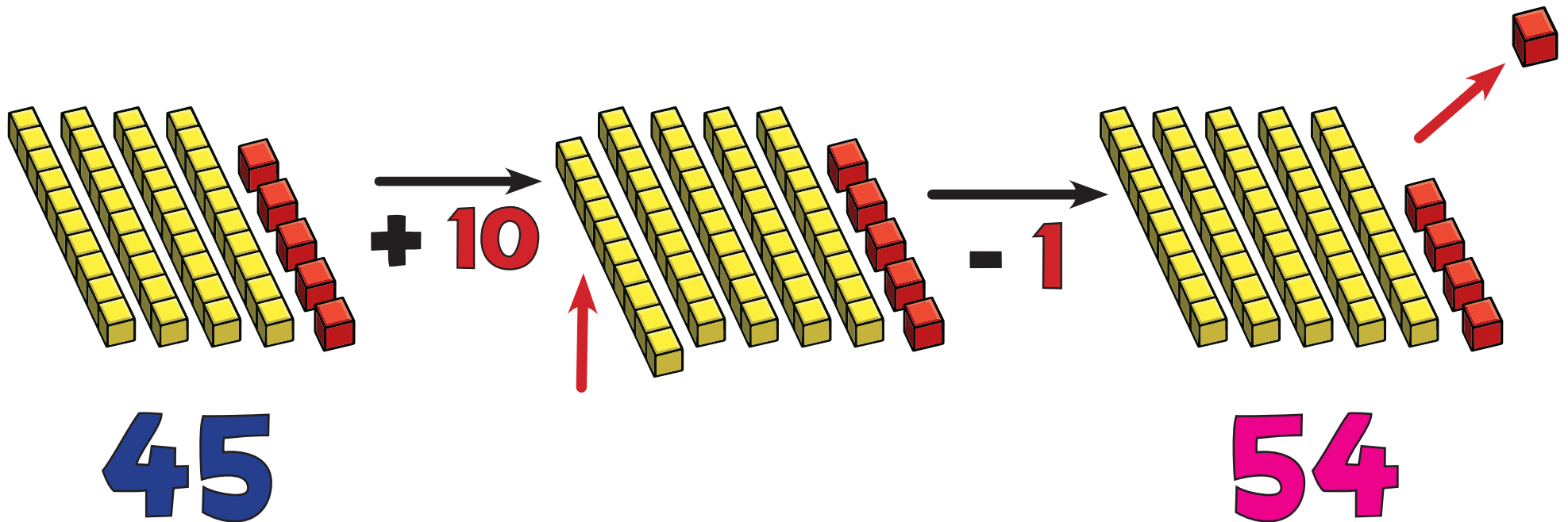


MA2: Round & Adjust



MC RaPa CoDa Numbo
Visualisation

$$45 + 9 = 54$$



MA2: Round & Adjust



MC RaPa CoDa Numbo

1

$$45 + 9 = 54$$

$$45 + 10 - 1 =$$

$$55 - 1 = 54$$



MA2: Round & Adjust



MC RaPa CoDa Numbo

2

$$45 + 19 = 64$$

$$45 + 20 - 1$$

$$65 - 1 = 64$$



MA2: Round & Adjust



MC RaPa CoDa Numbo

3

$$45 + 97 = 142$$

$$45 + 100 - 3$$

$$145 - 3 = 142$$



MA2: Round & Adjust



MC RaPa CoDa Numbo

4

$$345 + 298 = 643$$

$$345 + 300 - 2$$

$$645 - 2 = 643$$



MA2: Round & Adjust



MC RaPa CoDa Numbo

5

$$4645 + 1996 = 6641$$

$$4645 + 2000 - 4$$

$$6645 - 4 = 6641$$



MA2: Round & Adjust



MC RaPa CoDa Numbo

6

$$45.2 + 49.9 = 95.1$$

$$45.2 + 50 - 0.1$$

$$95.2 - 0.1 = 95.1$$



MA3: Partitioning



MC RaPa CoDa Numbo

$$45 + 82 = 127$$

$$120 + 7 = 127$$



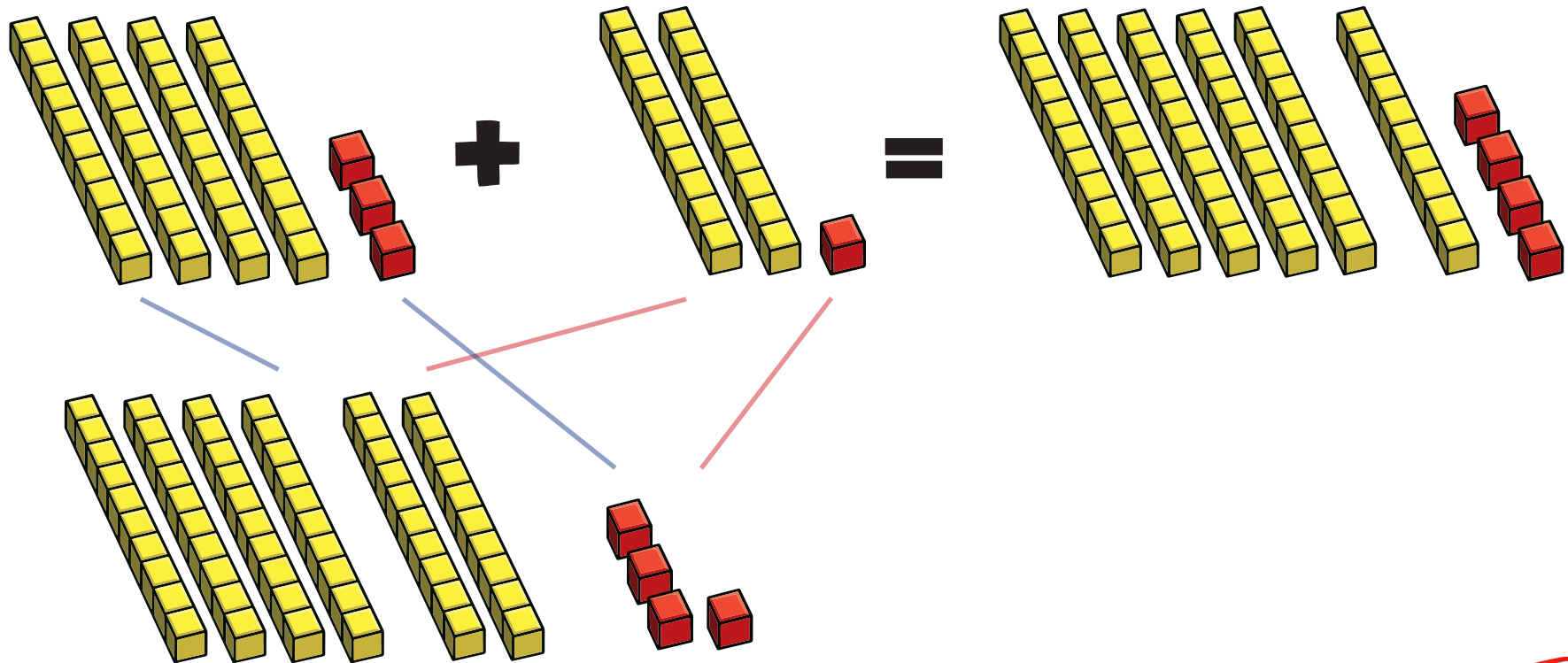
MA3: Partitioning

Visualisation



MC RaPa CoDa Numbo
Visualisation

$$43 + 21 = 64$$



MA3: Partitioning



MC RaPa CoDa Numbo

1

$$8 + 6 = 14$$

$$8 + 2 + 4 = 14$$



MA3: Partitioning



MC RaPa CoDa Numbo

2

$$43 + 21 = 64$$

$$60 + 4 = 64$$



MA3: Partitioning



MC RaPa CoDa Numbo

3

$$57 + 25 = 82$$

$$70 + 12 = 82$$



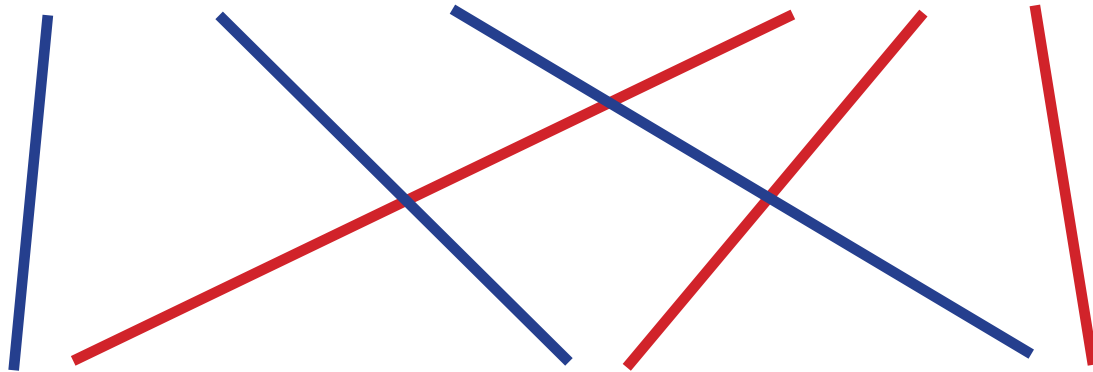
MA3: Partitioning



MC RaPa CoDa Numbo

4

$$648 + 231 = 879$$



$$800 + 70 + 9 = 879$$



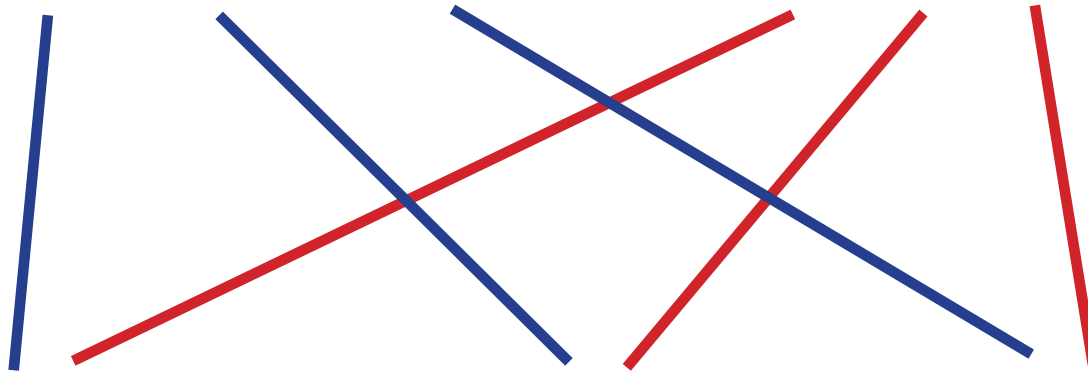
MA3: Partitioning



MC RaPa CoDa Numbo

5

$$576 + 258 = 834$$



$$700 + 120 + 14 = 834$$



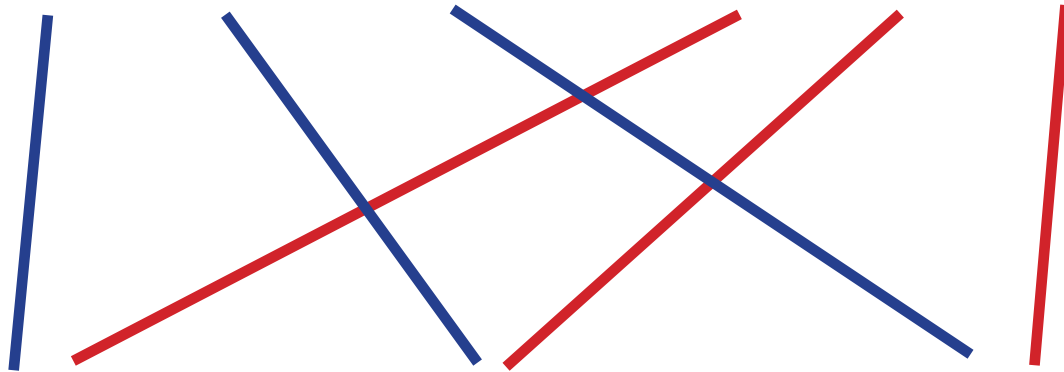
MA3: Partitioning



MC RaPa CoDa Numbo

6

$$4.73 + 2.21 = 6.94$$



$$6 + 0.9 + 0.04 = 6.94$$

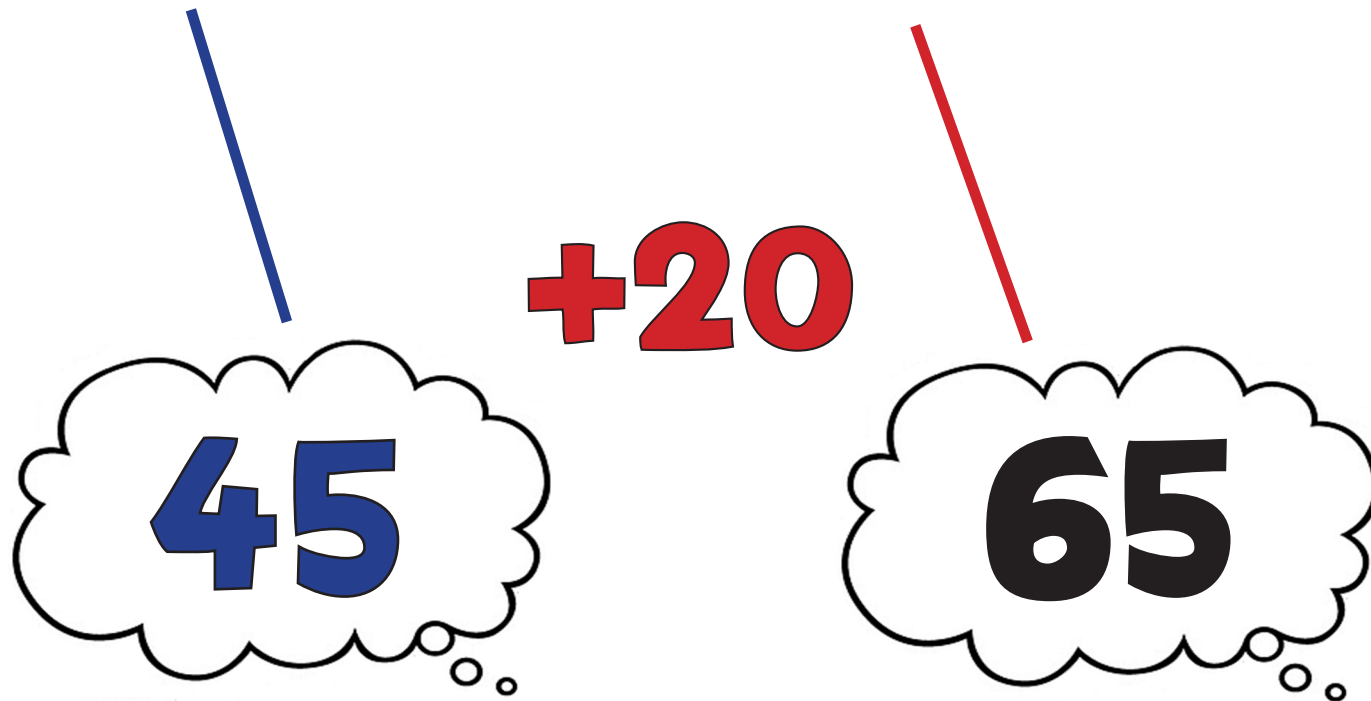


MA4: Counting On



MC RaPa CoDa Numbo

$$45 + 20 = 65$$

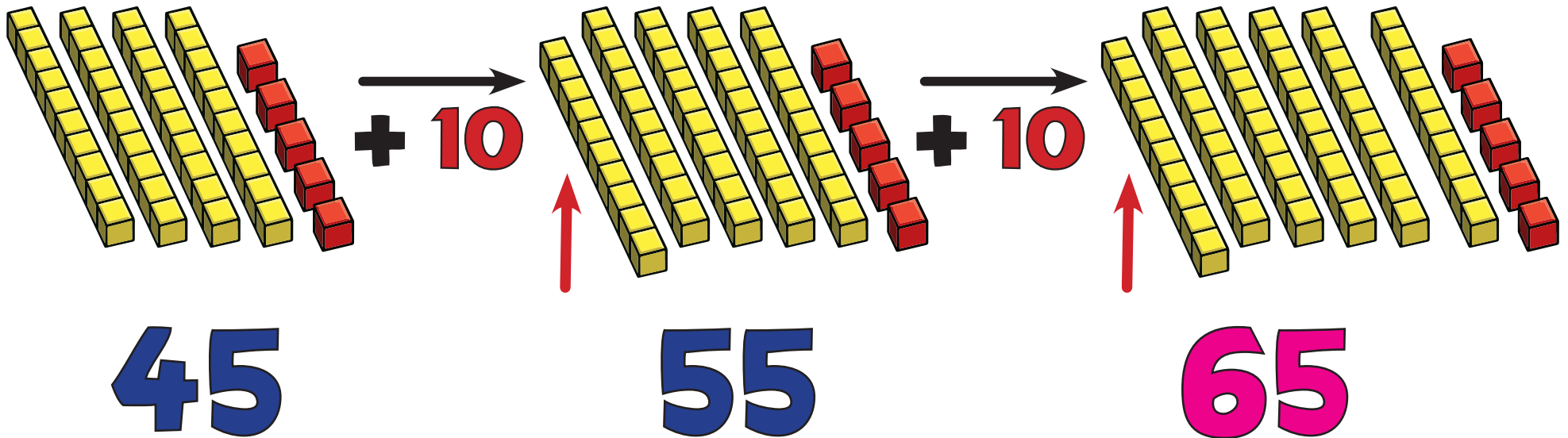


MA4: Counting On



MC RaPa CoDa Numbo
Visualisation

$$45 + 20 = 65$$



MA4a: Counting On

Ones



MC RaPa CoDa Numbo

1

$$12 + 5 = 17$$



+5



MA4b: Counting On

Tens



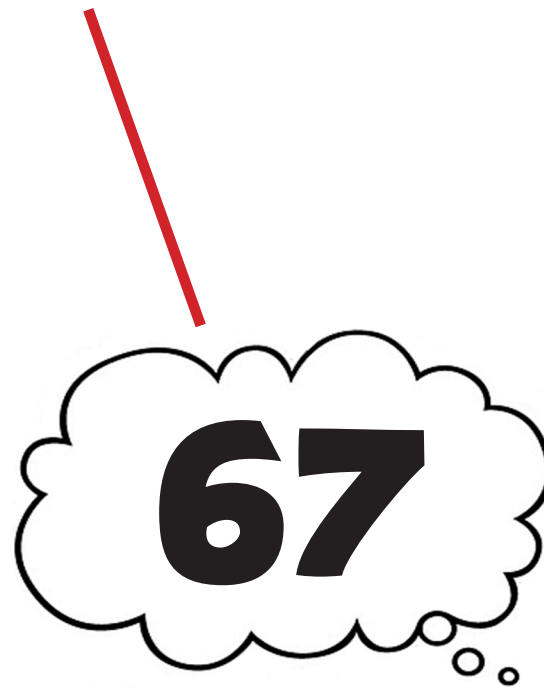
MC RaPa CoDa Numbo

1

$$57 + 10 = 67$$



+10



MA4a: Counting On

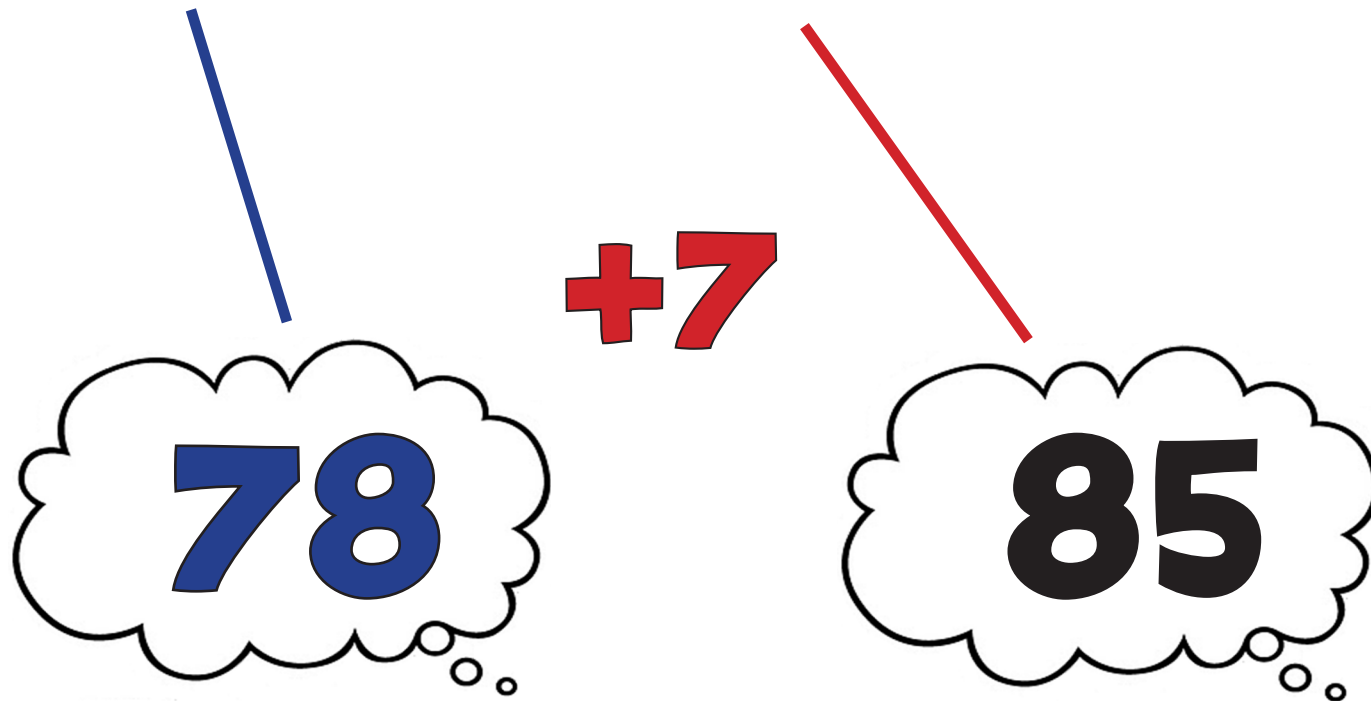
Ones



MC RaPa CoDa Numbo

2

$$78 + 7 = 85$$



MA4b: Counting On

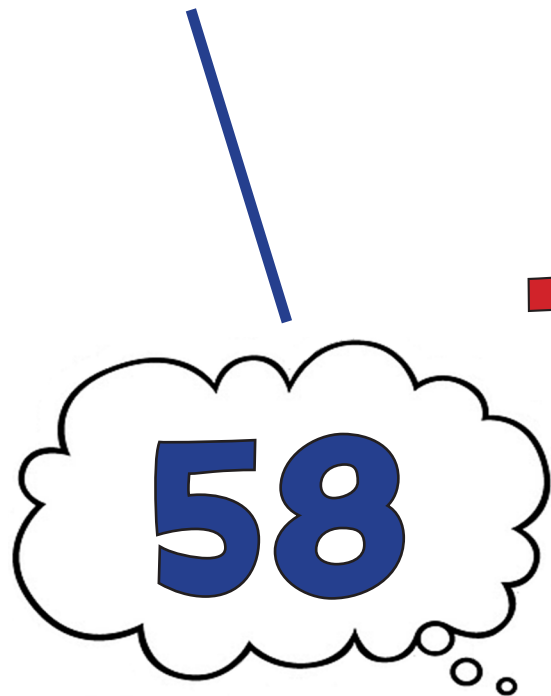
Tens



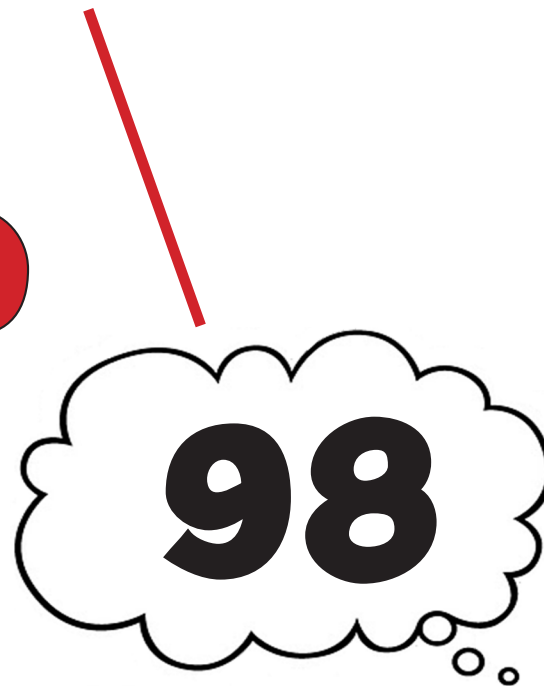
MC RaPa CoDa Numbo

2

$$58 + 40 = 98$$



+40



MA4a: Counting On

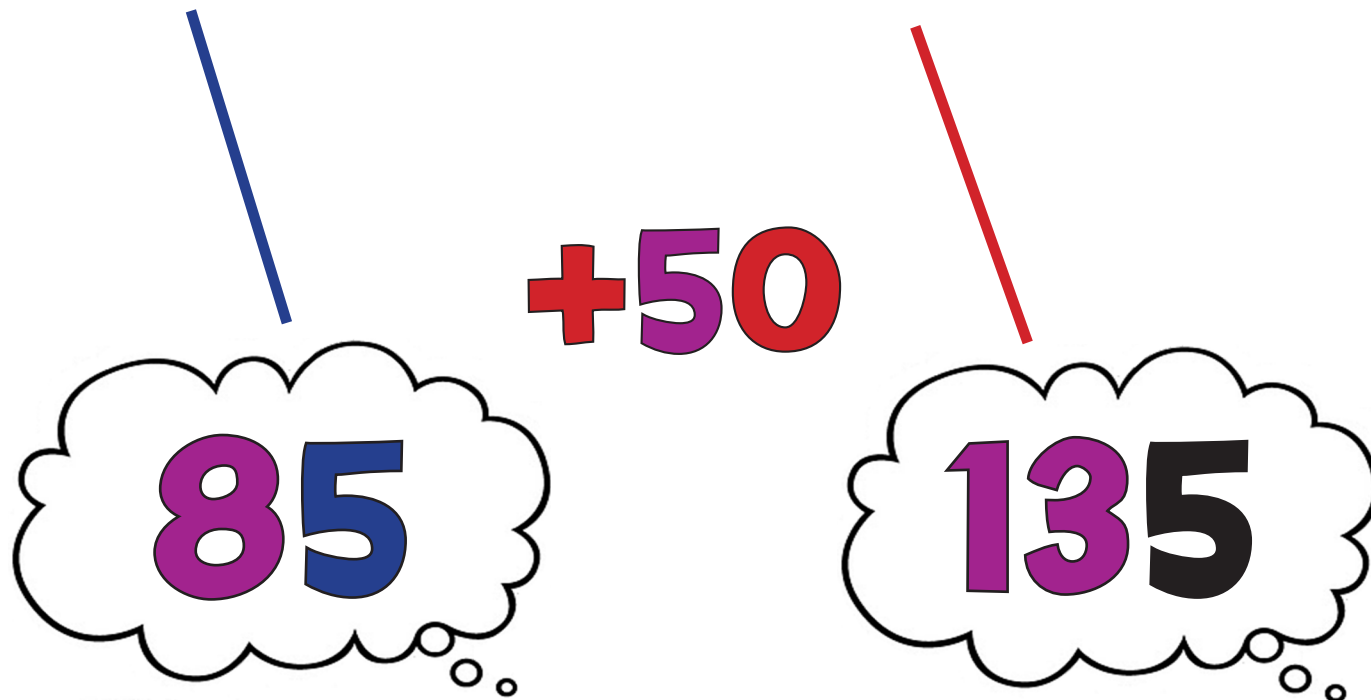
Tens



MC RaPa CoDa Numbo

3

$$85 + 50 = 135$$

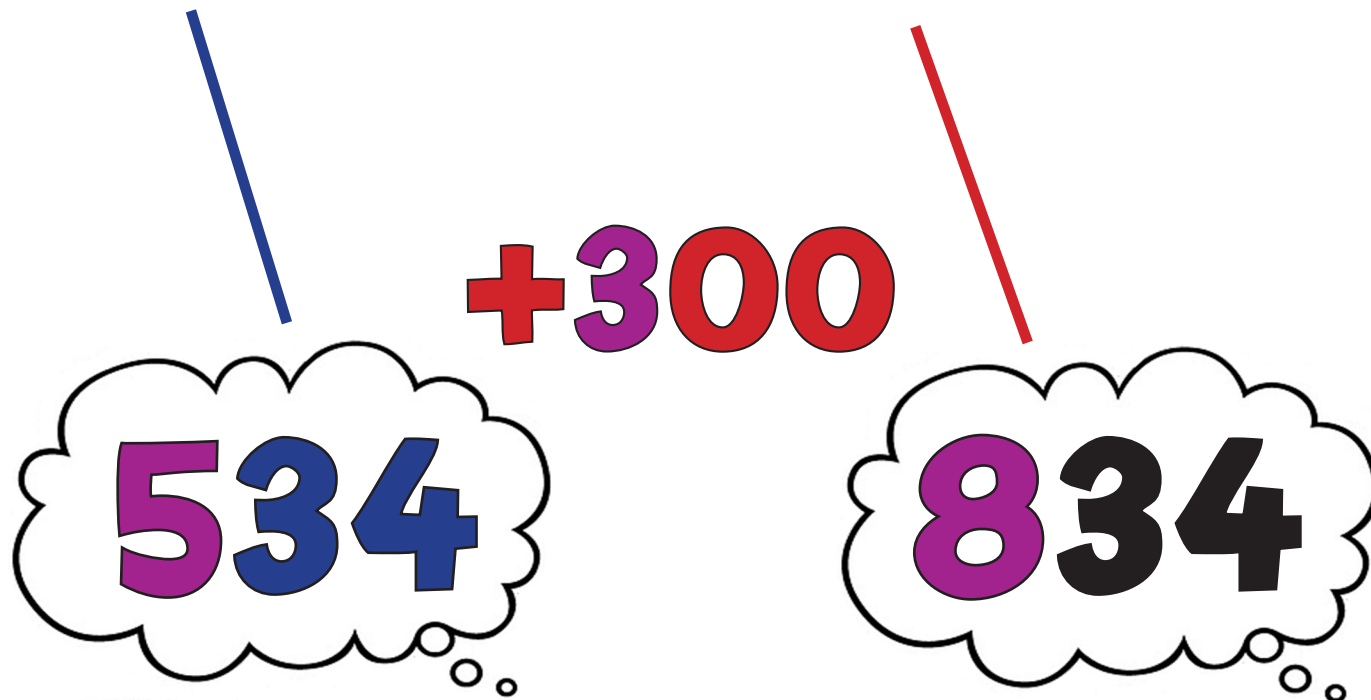


MA4b: Counting On

MC RaPa CoDa Numbo
3

Hundreds

$$534 + 300 = 834$$



MA4a: Counting On

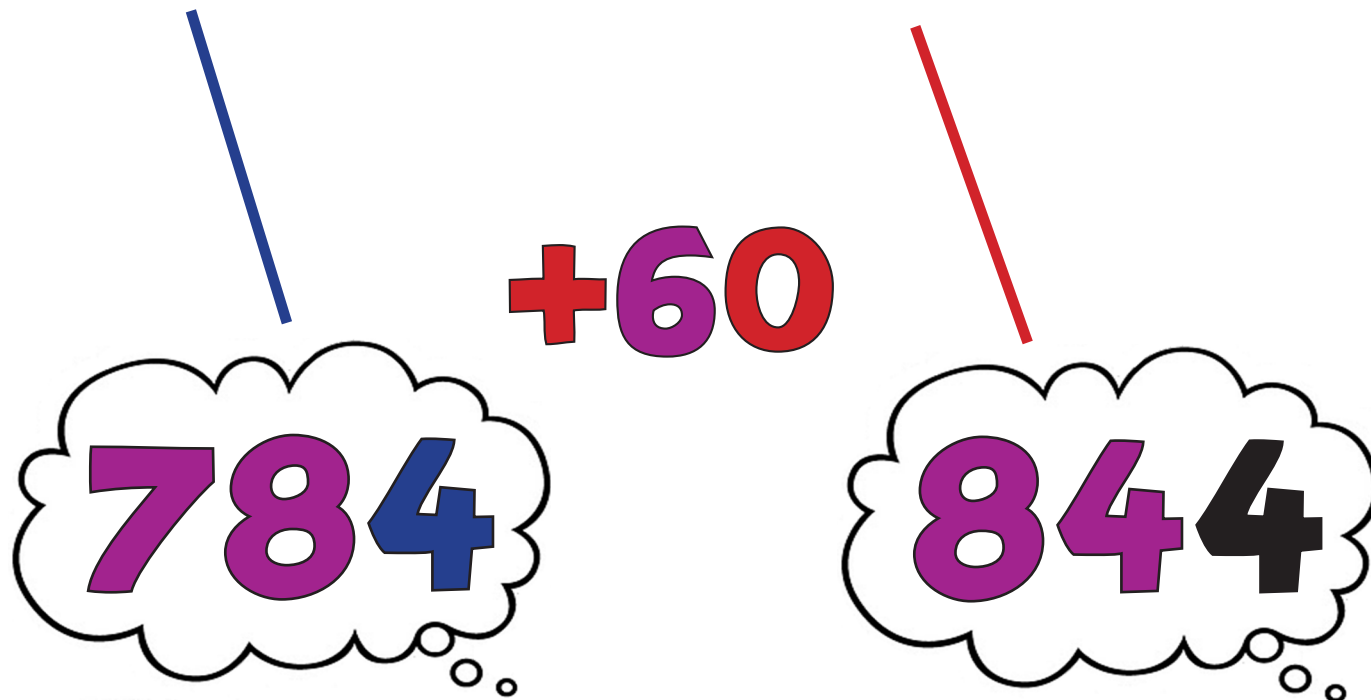
Tens



MC RaPa CoDa Numbo

4

$$784 + 60 = 844$$



MA4b: Counting On

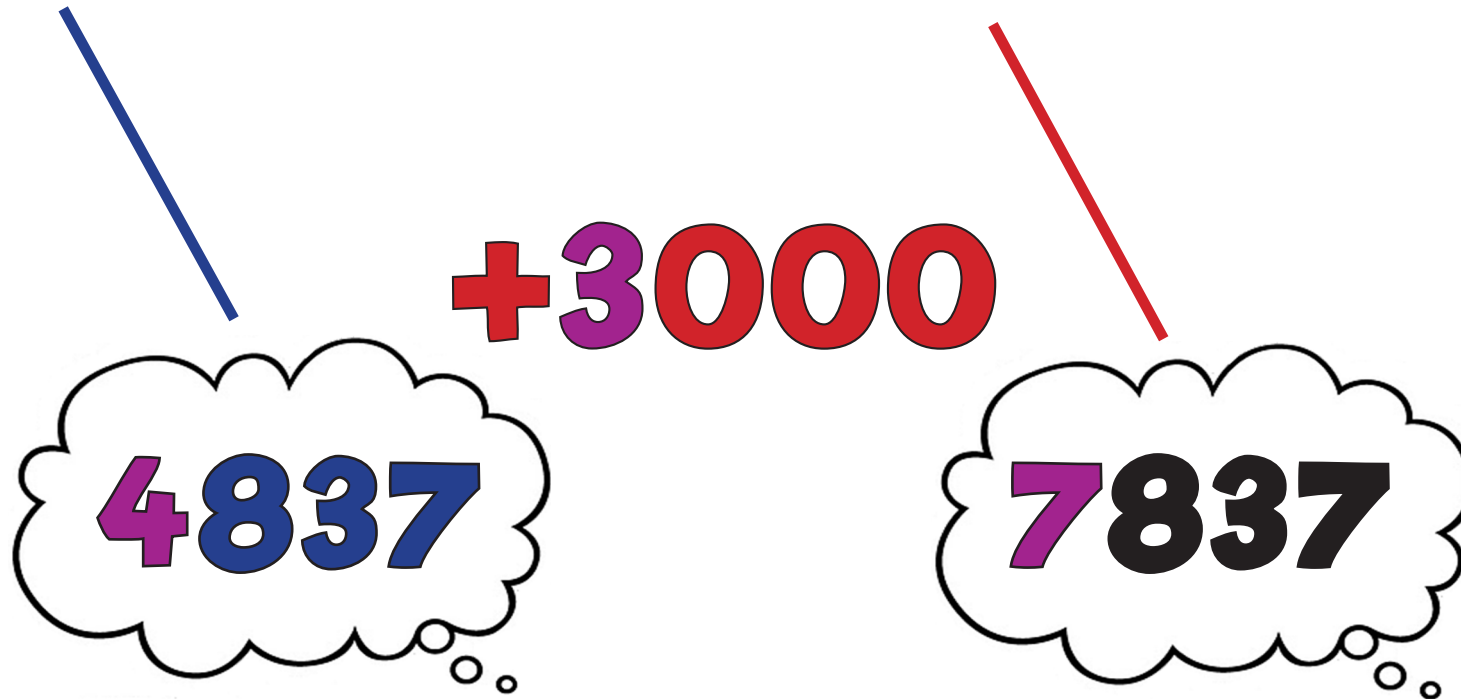
Hundreds



MC RaPa CoDa Numbo

4

$$4837 + 3000 = 7837$$

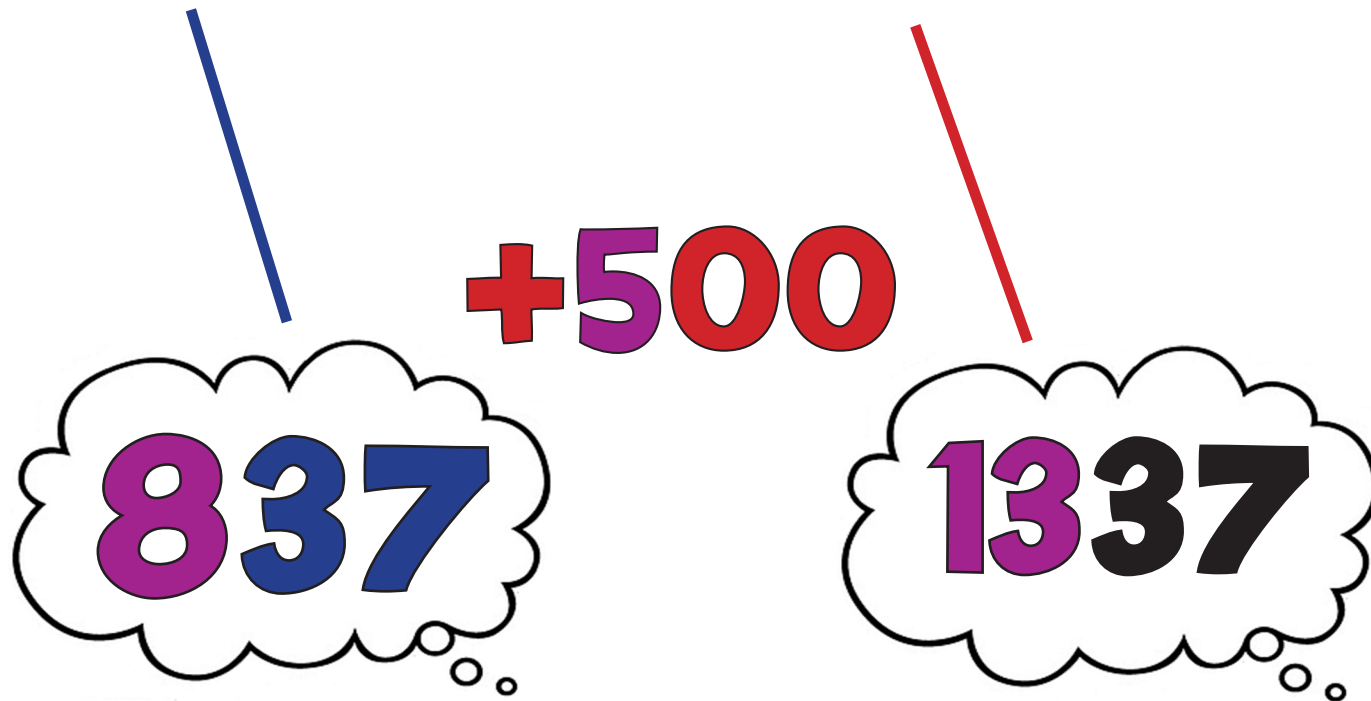


MA4a: Counting On

MC RaPa CoDa Numbo
5

Hundreds

$$837 + 500 = 1337$$



MA4b: Counting On

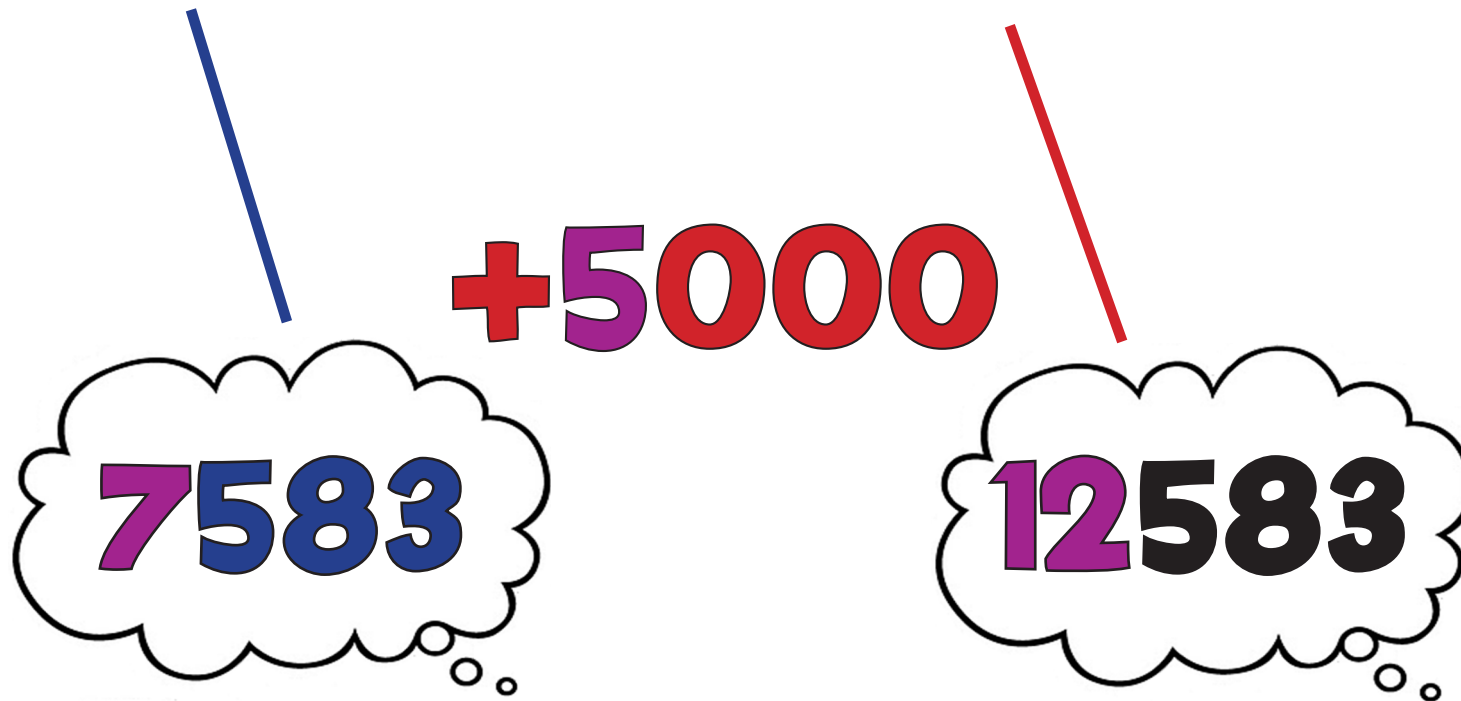
Thousands



MC RaPa CoDa Numbo

5

$$7583 + 5000 = 12583$$



MA4a: Counting On



MC RaPa CoDa Numbo

6

Ten Thousands

$$43,826 + 30,000 = 73,826$$

43,826

+30,000

73,826



MA4b: Counting On

Millions



MC RaPa CoDa Numbo

6

$$5,763,947 + 4,000,000 = 9,763,947$$

+4,000,000

5,763,947

9,763,947



MA5: Double & Adjust



MC RaPa CoDa Numbo

$$45 + 46 = 91$$

45

1

$$90 + 1 = 91$$

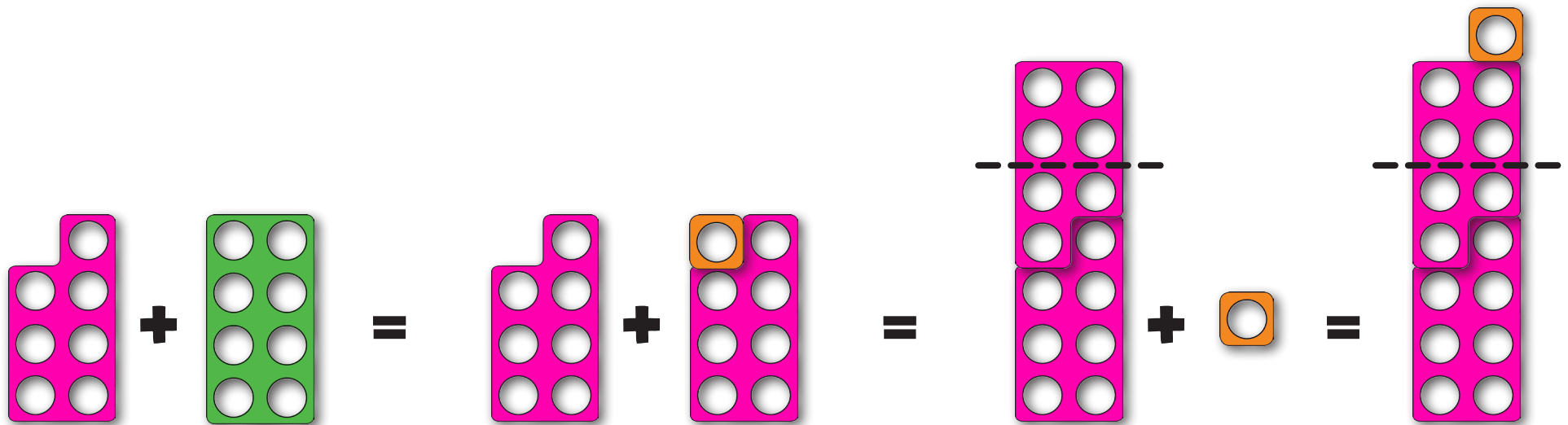


MA5: Double & Adjust



MC RaPa CoDa Numbo
Visualisation

$$7 + 8 = 15$$



$$7 + 8 = 7 + 7 + 1 = 14 + 1 = 15$$



MA5: Double & Adjust



MC RaPa CoDa Numbo

1

$$5 + 6 = 11$$

A diagram illustrating the 'Double & Adjust' strategy. The number 5 is shown in blue. The number 6 is shown in red and circled in red. A dotted line connects the 5 to the 6. Below the 6, the number 5 is circled in red, and the number 1 is circled in red. Lines connect the 6 to both the 5 and the 1, showing that 6 is decomposed into 5 and 1.

$$10 + 1 = 11$$

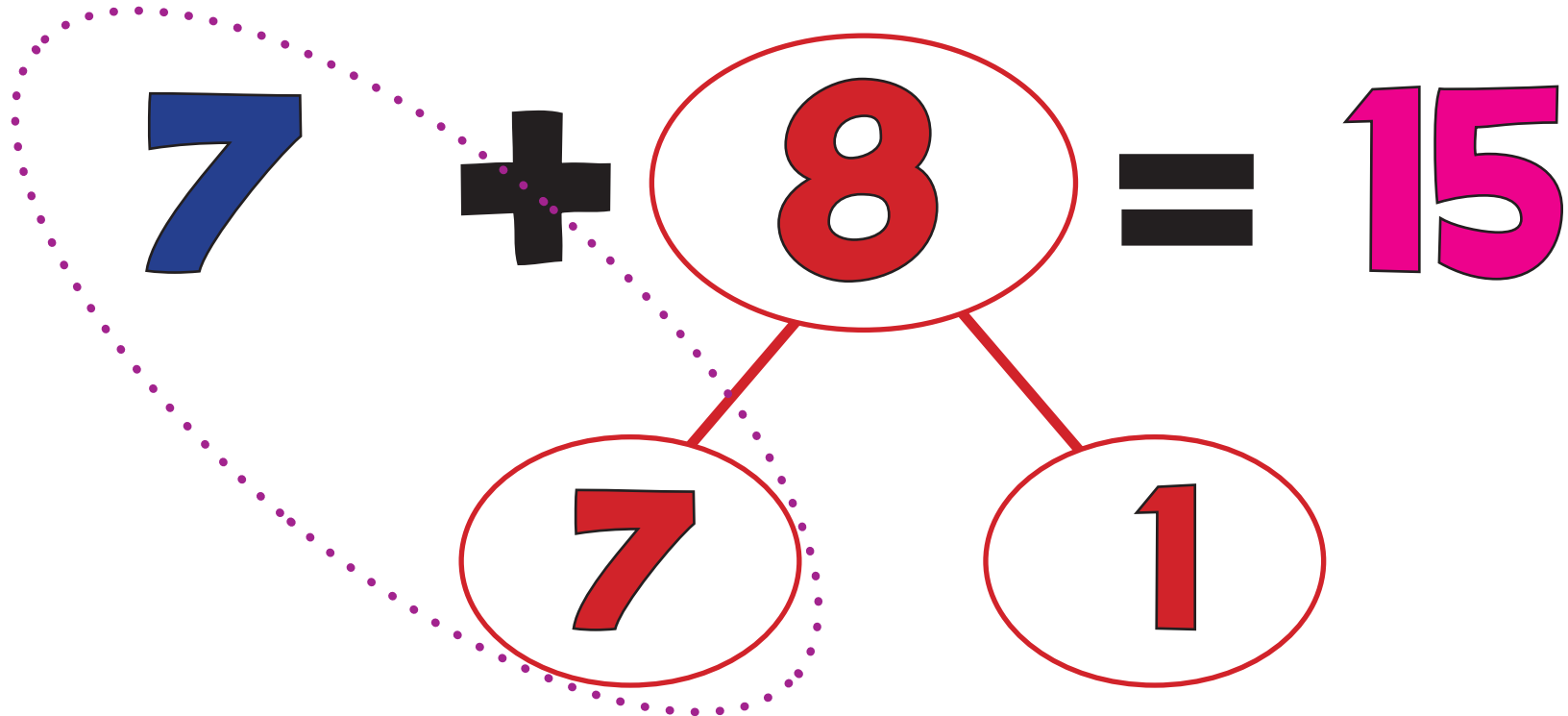


MA5: Double & Adjust



MC RaPa CoDa Numbo

2



$$14 + 1 = 15$$

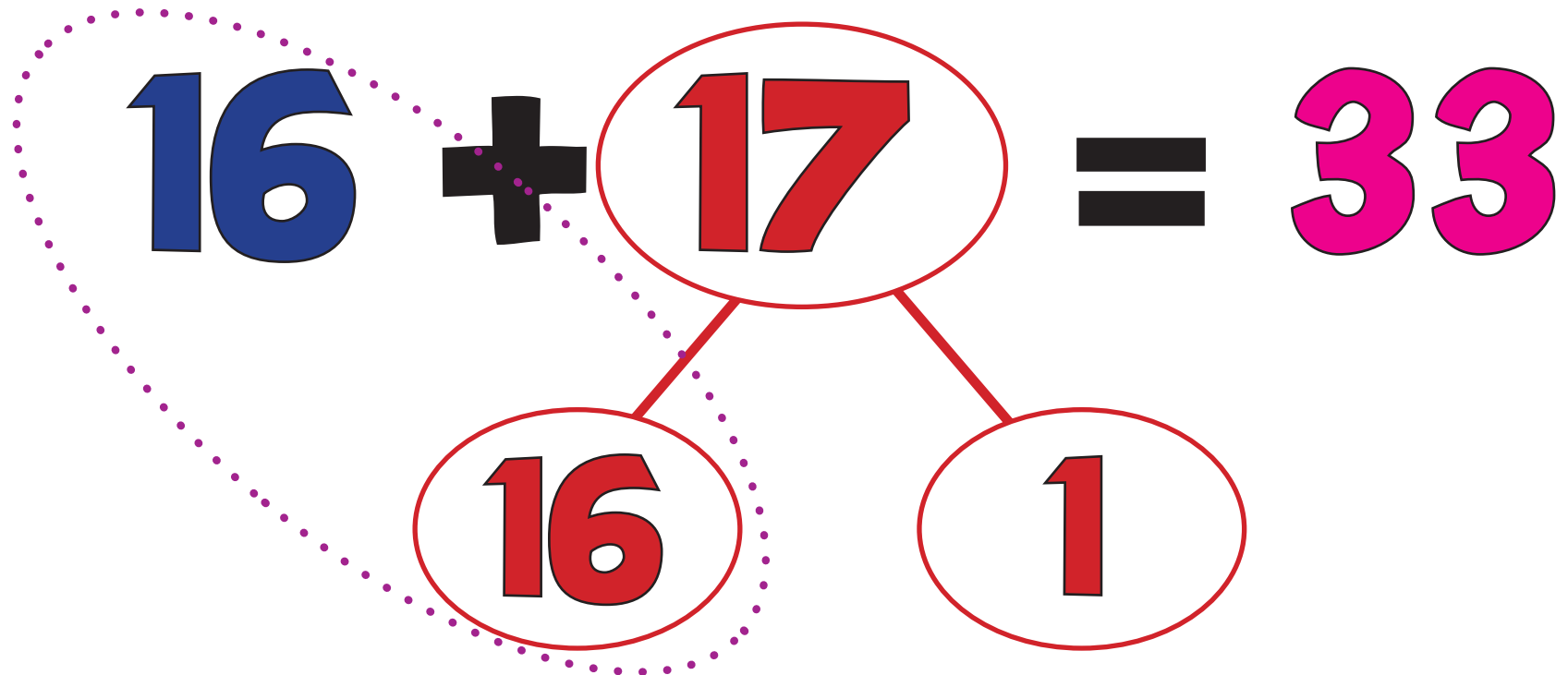


MA5: Double & Adjust



MC RaPa CoDa Numbo

3



$$32 + 1 = 33$$



MA5: Double & Adjust



MC RaPa CoDa Numbo

4

$$37 + 38 = 75$$

A diagram illustrating the 'Double & Adjust' strategy. The number 37 is shown in blue. The number 38 is circled in red. A dotted line connects 37 to 38. Below 38, two red circles are connected by lines: one containing 37 and one containing 1. A dotted line also connects 37 to the 37 in the lower circle.

$$74 + 1 = 75$$



MA5: Double & Adjust



MC RaPa CoDa Numbo

5

$$125 + 127 = 252$$

125

2

$$250 + 2 = 252$$



MA5: Double & Adjust



MC RaPa CoDa Numbo

6

$$4.5 + 4.7 = 9.2$$

4.5

0.2

$$9 + 0.2 = 9.2$$

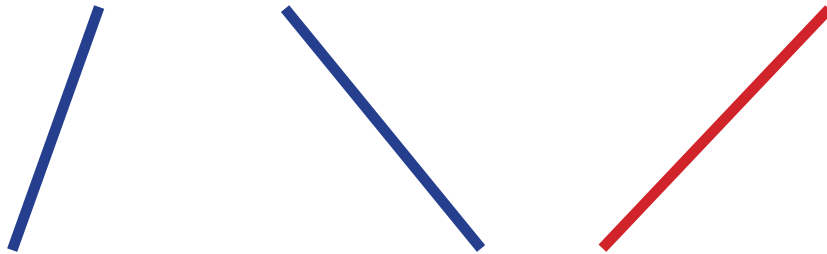


MA6: Number Bonds



MC RaPa CoDa Numbo

$$45 + 95 = 140$$



$$40 + 100 = 140$$

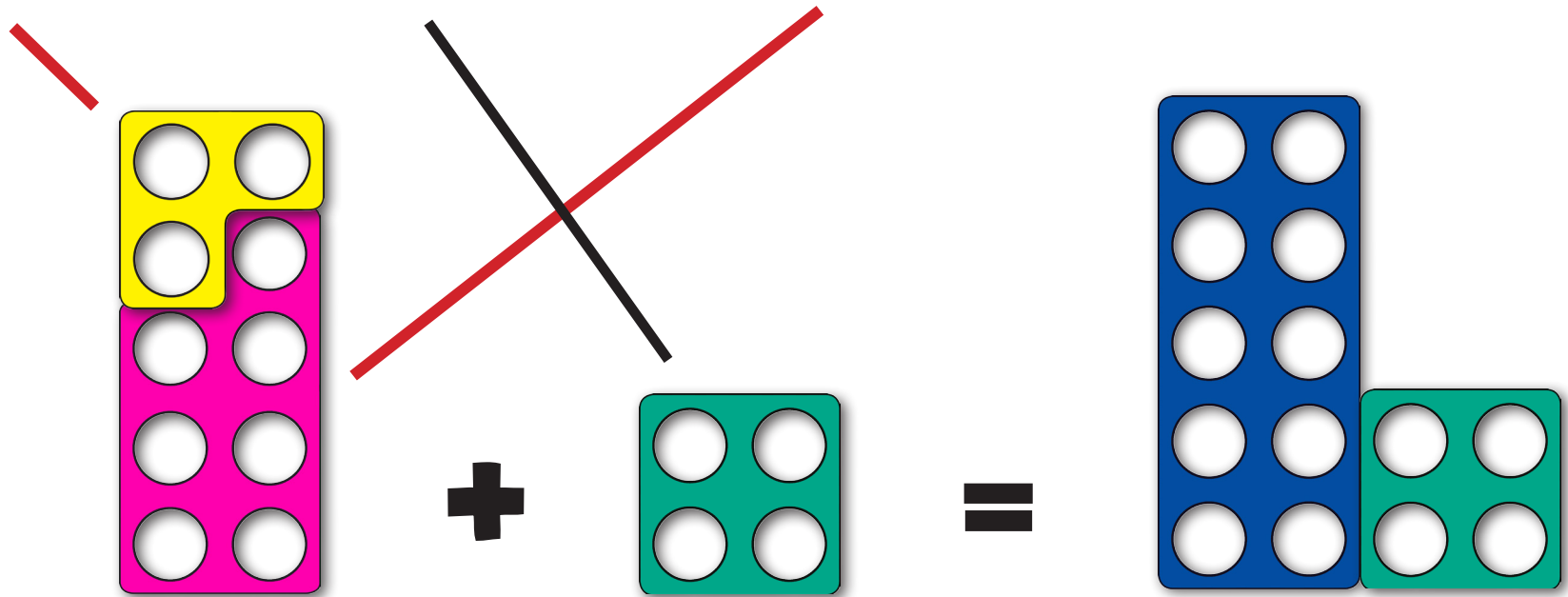


MA6: Number Bonds



MC RaPa CoDa Numbo
Visualisation

$$3 + 4 + 7 = 14$$



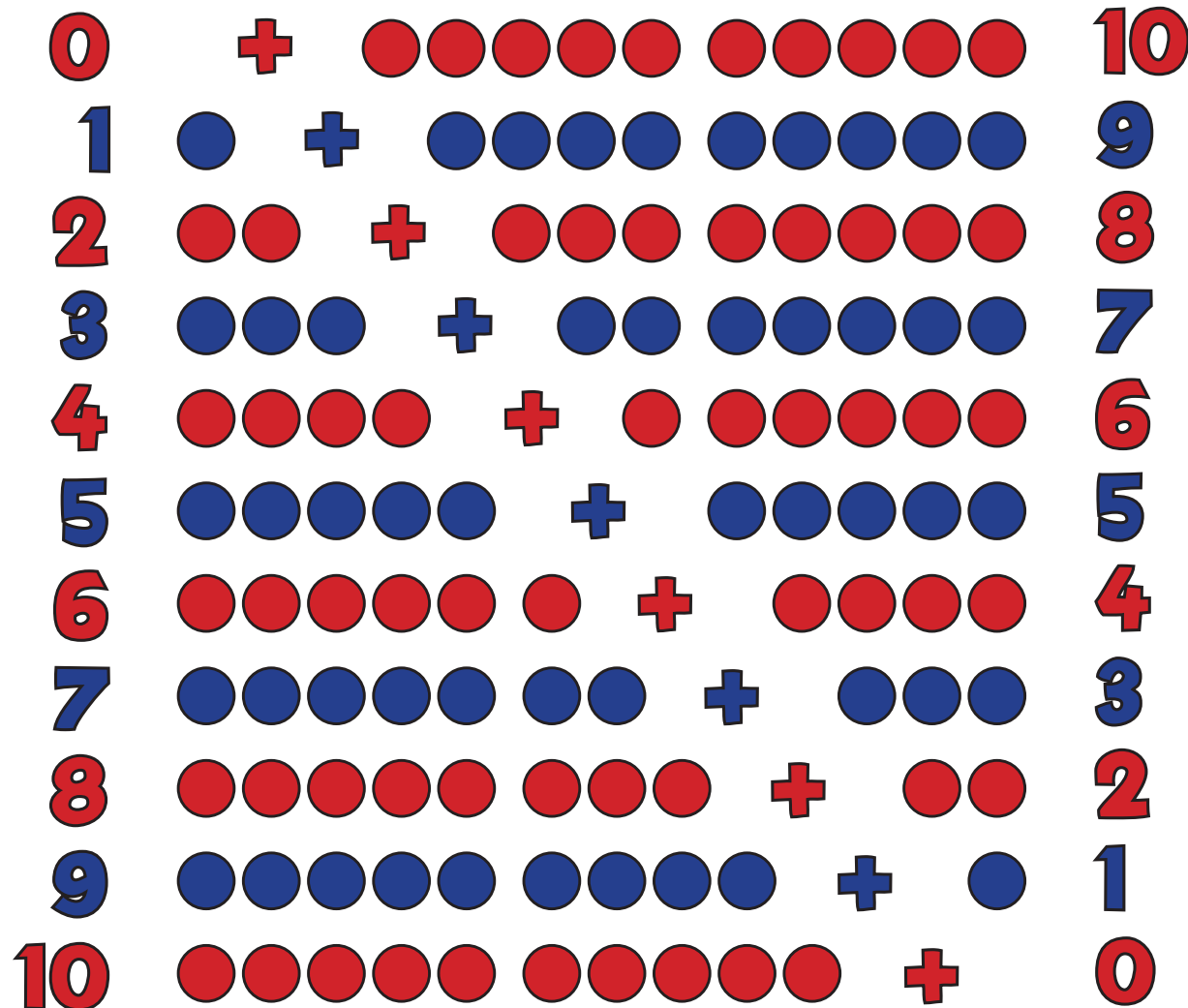
MA6: Number Bonds



MC RaPa CoDa Numbo

1

Learn Bonds



0	+	10	=	10
1	+	9	=	10
2	+	8	=	10
3	+	7	=	10
4	+	6	=	10
5	+	5	=	10
6	+	4	=	10
7	+	3	=	10
8	+	2	=	10
9	+	1	=	10
10	+	0	=	10



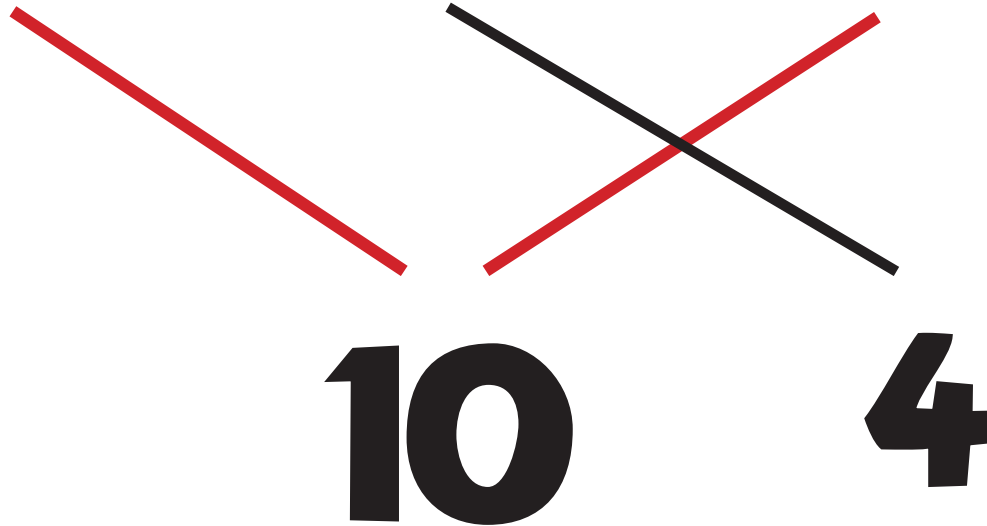
MA6: Number Bonds



MC RaPa CoDa Numbo

2

$$3 + 4 + 7 = 14$$



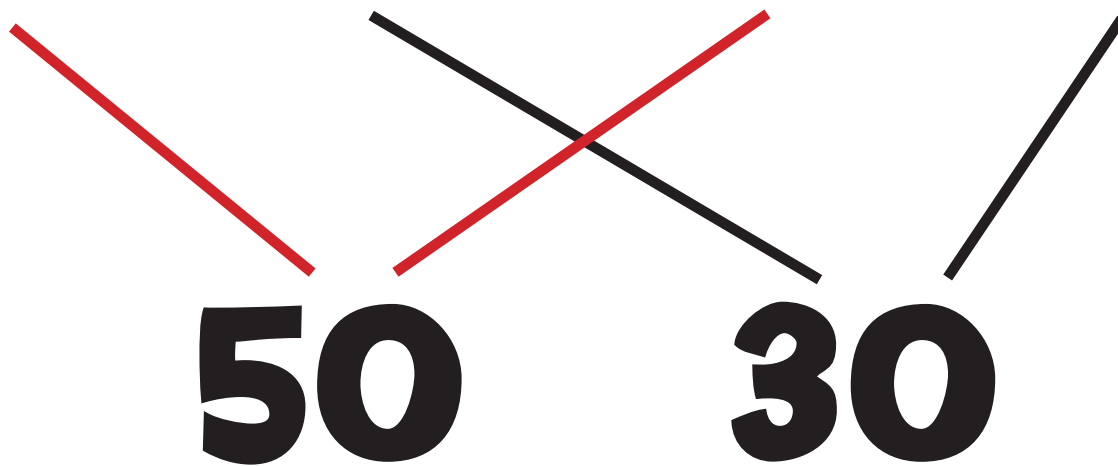
MA6: Number Bonds



MC RaPa CoDa Numbo

3

$$43 + 9 + 7 + 21 = 80$$



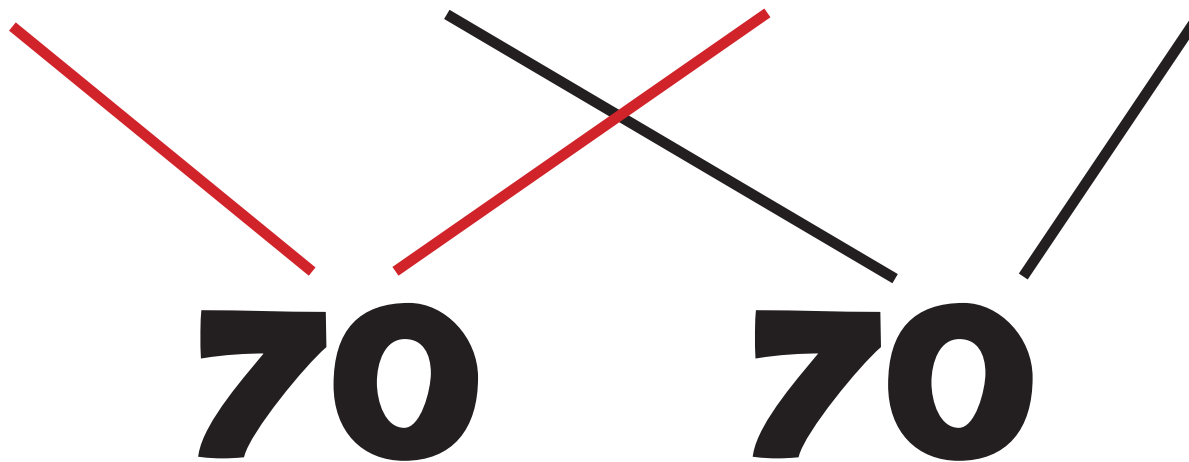
MA6: Number Bonds



MC RaPa CoDa Numbo

4

$$42 + 16 + 28 + 54 = 140$$



MA6: Number Bonds



MC RaPa CoDa Numbo

5

$$£4.56 + £3.27 + £1.44 = £9.27$$

$$£6.00 \quad £3.27$$



MA6: Number Bonds



MC RaPa CoDa Numbo

6

$$24.25 + 31.63 + 21.75 = 77.63$$

46

31.63



MC RaPa CoOCoB NumFa

69 **MS1** **MC** = Manipulate Calculation

77 **MS2** **Ra** = Round and Adjust

85 **MS3** **Pa** = Partitioning

91 **MS4** **CoO** = Counting On

108 **MS5** **CoB** = Counting Back

123 **MS6** **NumFa** = Number Facts



6 Cool Strategies for Mental Subtraction!



MS1: Manipulate Calculation



MC RaPa CoOCoB NumFa

$$84 - 29 = 55$$



$$85 - 30 = 55$$



MS1: Manipulate Calculation

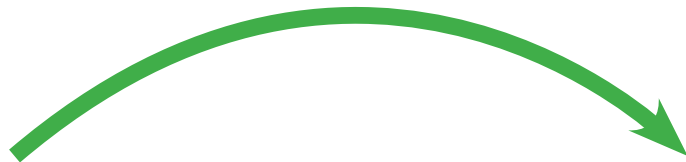


MC RaPa CoOCoB NumFa
Visualisation

Same Difference!

$$24 - 9 = 15$$

+15



$$\begin{array}{r} 9 \\ \hline 24 \end{array}$$

=

+15



$$\begin{array}{r} 10 \\ \hline 25 \end{array}$$

$$24 - 9 = 25 - 10$$

$$(24 + 1) - (9 + 1)$$



MS1: Manipulate Calculation

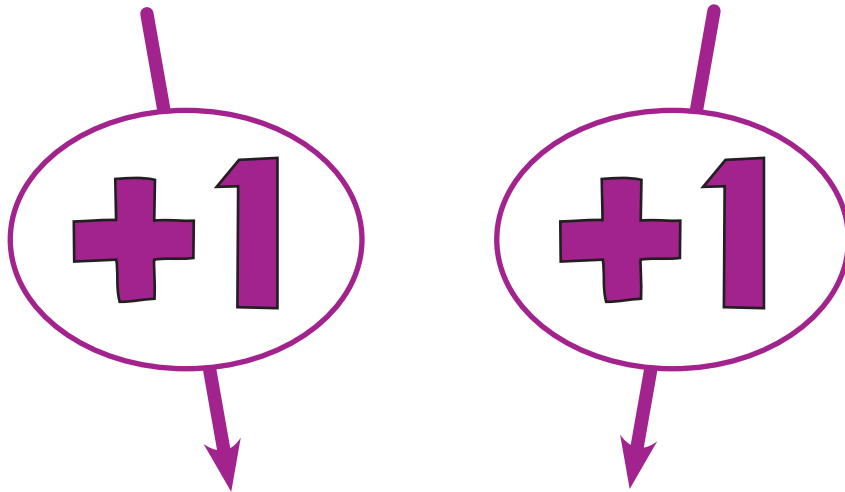
Same Difference!



MC RaPa CoOCoB NumFa

1

$$24 - 9 = 15$$



$$25 - 10 = 15$$



MS1: Manipulate Calculation

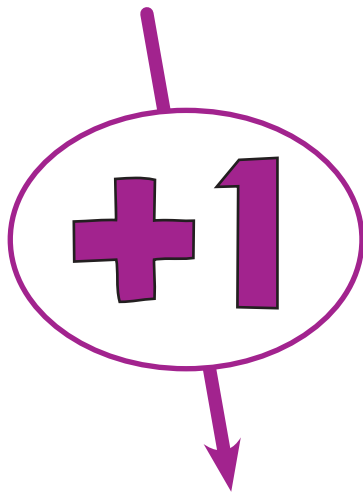


MC RaPa CoOCoB NumFa

2

Same Difference!

$$84 - 29 = 55$$



$$85 - 30 = 55$$



MS1: Manipulate Calculation



MC RaPa CoOCoB NumFa

3

Same Difference!

$$463 - 97 = 366$$



$$466 - 100 = 366$$



MS1: Manipulate Calculation



MC RaPa CoOCoB NumFa

4

Same Difference!

$$876 - 298 = 578$$



$$878 - 300 = 578$$



MS1: Manipulate Calculation



MC RaPa CoOCaB NumFa

5

Same Difference!

$$5864 - 2996 = 2868$$



$$5868 - 3000 = 2868$$



MS1: Manipulate Calculation



MC RaPa CoOCoB NumFa

6

Same Difference!

$$46357 - 11999 = 34358$$



$$46358 - 12000 = 34358$$



MS2: Round & Adjust



MC RaPa CoOCob NumFa

$$84 - 29 = 55$$

$$84 - 30 + 1$$

$$54 + 1 = 55$$

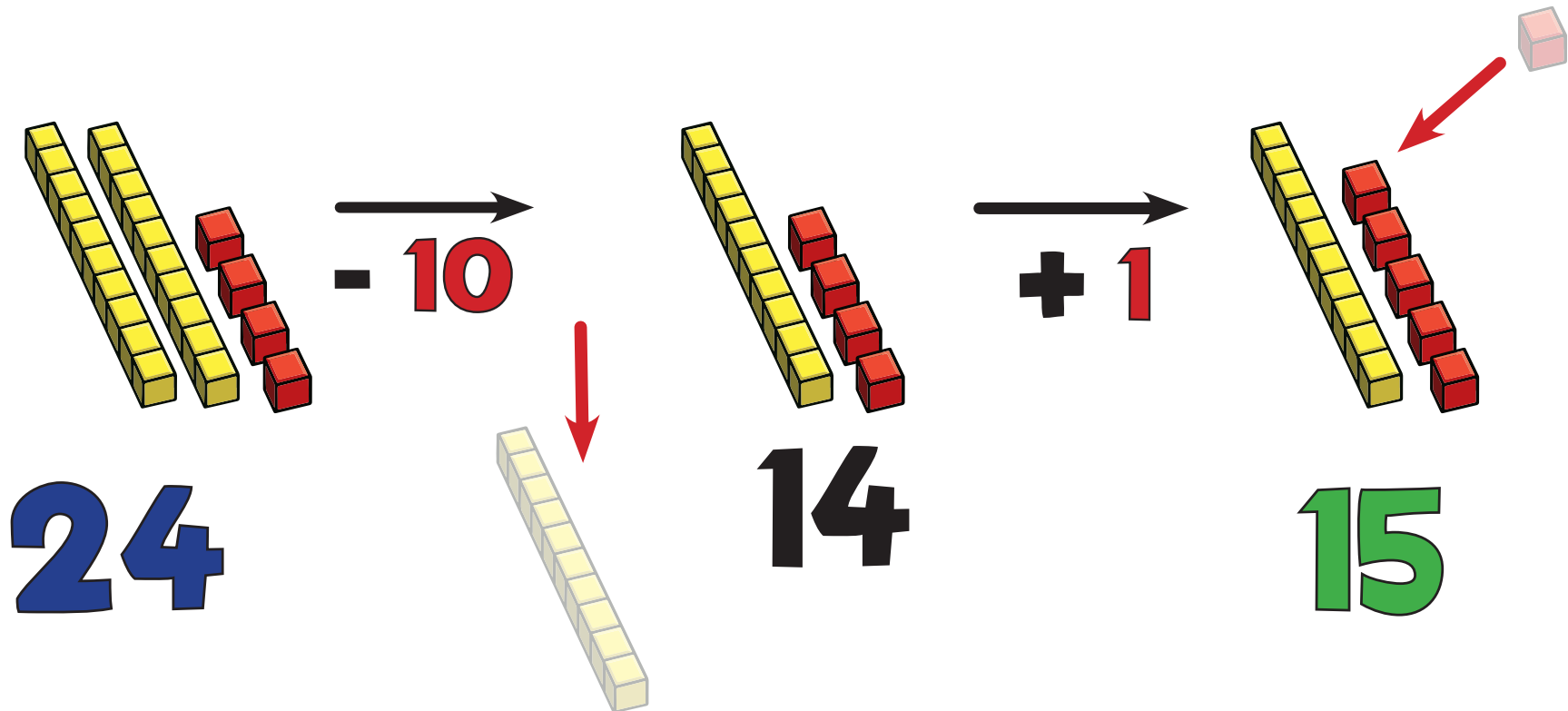


MS2: Round & Adjust



MC RaPa CoOCoB NumFa
Visualisation

$$24 - 9 = 15$$



MS2: Round & Adjust



MC RaPa CoOCoB NumFa

1

$$24 - 9 = 15$$

$$24 - 10 + 1$$

$$14 + 1 = 15$$



MS2: Round & Adjust



MC RaPa CoOCoB NumFa

2

$$84 - 29 = 55$$

$$84 - 30 + 1$$

$$54 + 1 = 55$$



MS2: Round & Adjust



MC RaPa CoOCoB NumFa

3

$$463 - 97 = 366$$

$$463 - 100 + 3$$

$$363 + 3 = 366$$



MA2: Round & Adjust



MC RaPa CoOCoB NumFa

4

$$876 - 298 = 578$$

$$876 - 300 + 2$$

$$576 + 2 = 578$$



MA2: Round & Adjust



MC RaPa CoOCoB NumFa

5

$$5864 - 2996 = 2868$$

$$5864 - 3000 + 4$$

$$2864 + 4 = 2868$$



MS2: Round & Adjust



MC RaPa CoOCoB NumFa

6

$$46357 - 11999 = 34358$$

$$46357 - 12000 + 1$$

$$46357 + 1 = 34358$$



MS3: Partitioning



MC RaPa CoOCoB NumFa

$$63 - 35 = 28$$

$$- 33 - 2$$



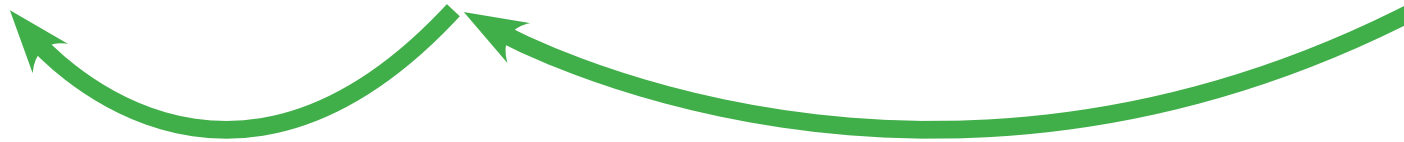
MS3: Partitioning



MC RaPa CoOCob NumFa
Visualisation

$$63 - 35 = 28$$

$$\begin{array}{ccc} 28 & 30 & 63 \\ \hline \end{array}$$



MS3: Partitioning



MC RaPa CoOCoB NumFa

1

$$23 - 8 = 15$$

$$- 3 - 5$$

23

20

15



MS3: Partitioning



MC RaPa CoOCoB NumFa

2

$$63 - 35 = 28$$

$$- 33 - 2$$



MS3: Partitioning



MC RaPa CoOCoB NumFa

3

$$123 - 28 = 95$$

$$- 23 - 5$$

123

100

95



MS3: Partitioning



MC RaPa CoOCoB NumFa

4

$$132 - 58 = 74$$

$$- 52 - 6$$

132

80

74



MS3: Partitioning



MC RaPa CoOCoB NumFa

5

$$750 - 372 = 378$$

$$- 350 - 22$$

750

400

378



MS3: Partitioning



MC RaPa CoOCoB NumFa

6

$$£64.30 - £24.50 = £39.80$$

$$- £24.30 - 20p$$

£64.30

£40

£39.80



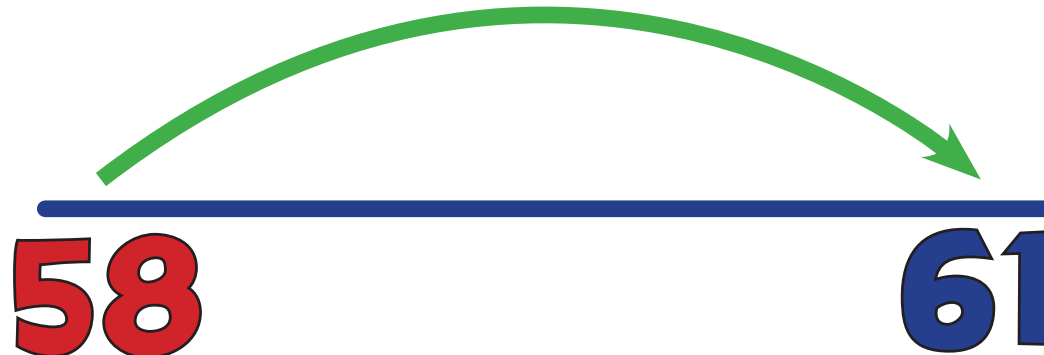
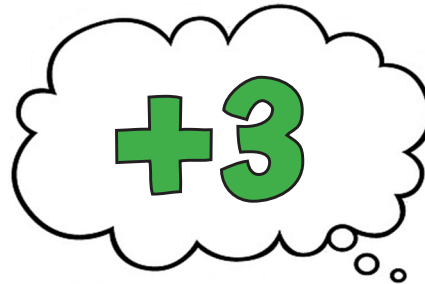
MS4a: Counting On



MC RaPa CoOCoB NumFa

Small Difference

$$61 - 58 = 3$$



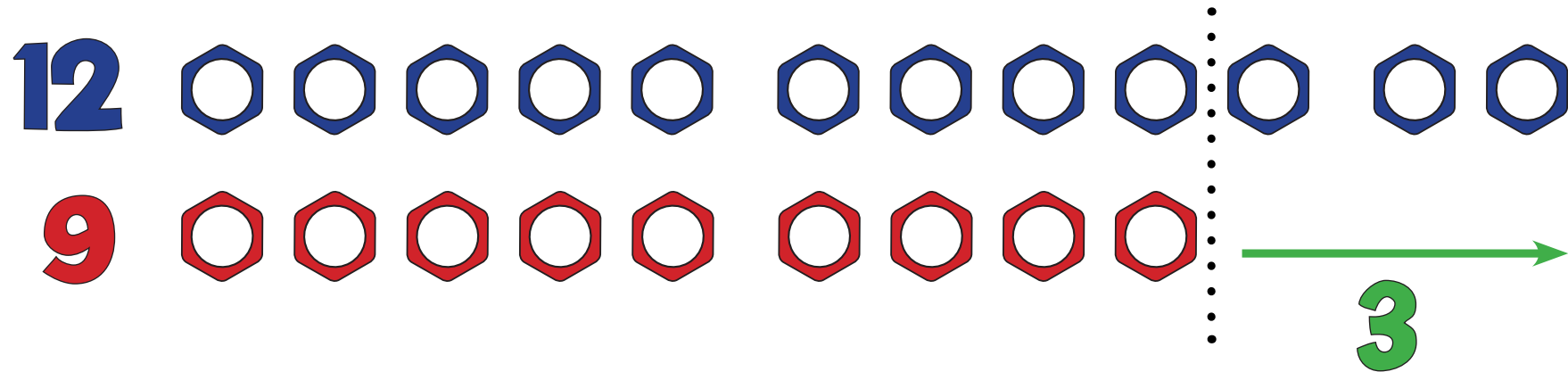
MS4a: Counting On



MC RaPa CoOCoB NumFa
Visualisation

Small Difference

$$12 - 9 = 3$$



MS4a: Counting On

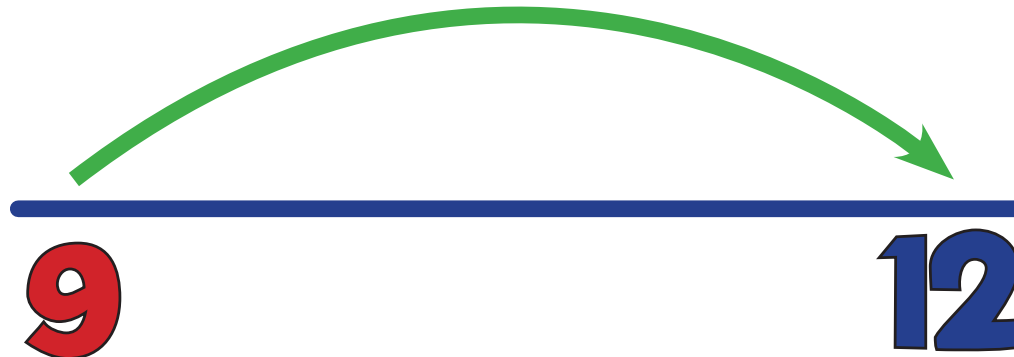
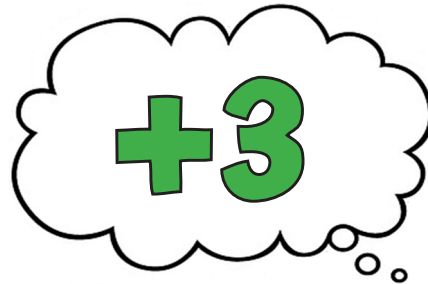


MC RaPa CoOCoB NumFa

1

Small Difference

$$12 - 9 = 3$$



MS4a: Counting On

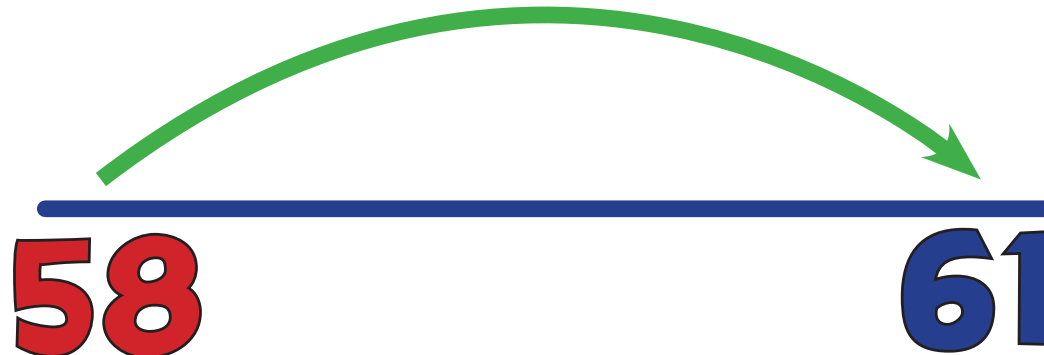
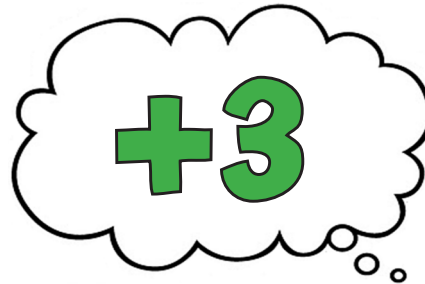


MC RaPa CoOCoB NumFa

2

Small Difference

$$61 - 58 = 3$$



MS4a: Counting On

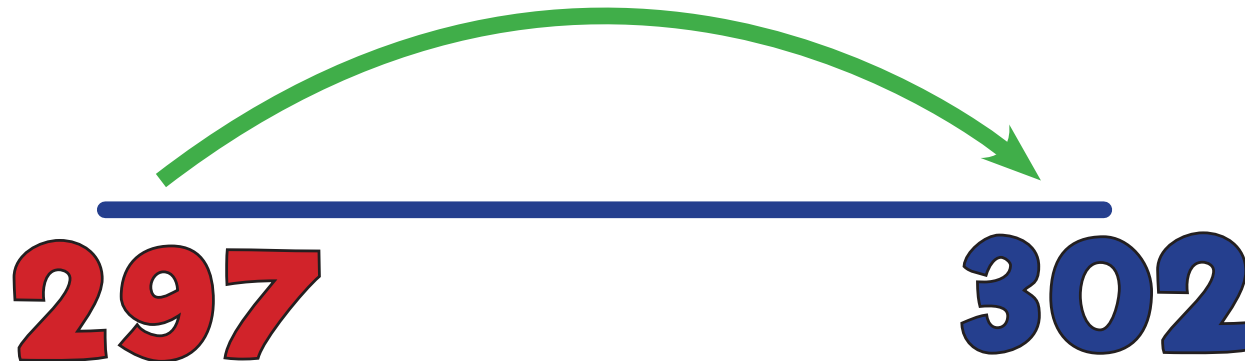


MC RaPa Co0CoB NumFa

3

Small Difference

$$302 - 297 = 5$$



MS4a: Counting On

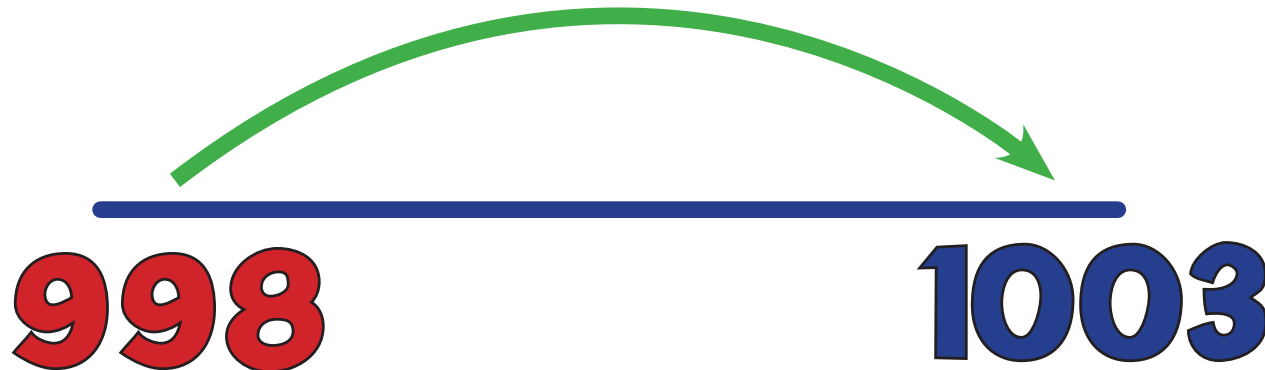


MC RaPa Co0CoB NumFa

4

Small Difference

$$1003 - 998 = 5$$



MS4a: Counting On



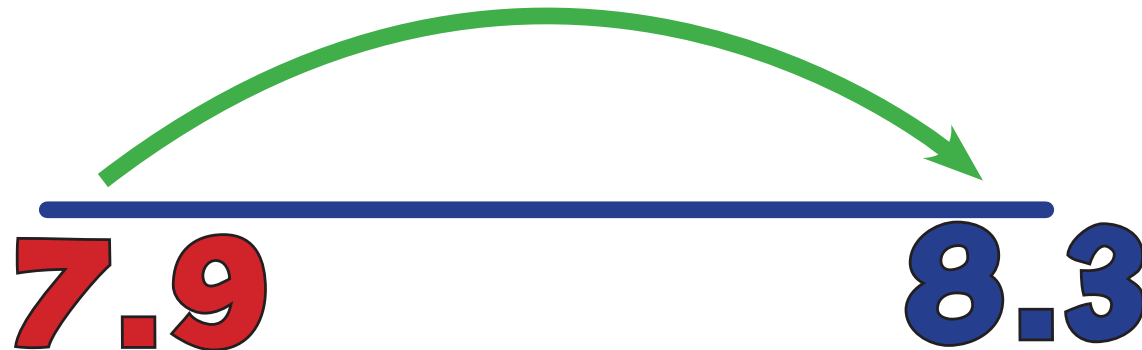
MC RaPa CoOCoB NumFa

5

Small Difference

$$8.3 - 7.9 = 0.4$$

+0.4



MS4a: Counting On



MC RaPa Co0CoB NumFa

6

Small Difference

$$€12.02 - €11.98 = 4p$$

+4p

€11.98

€12.02



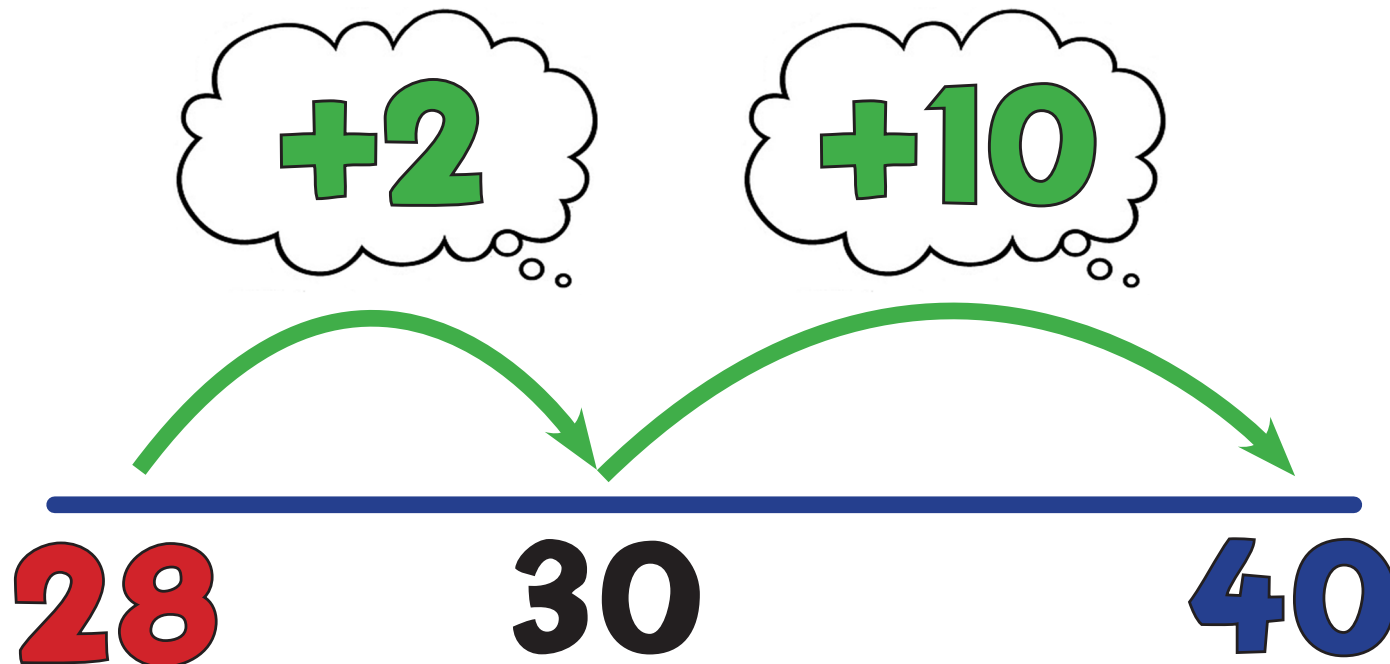
MS4b: Counting On



MC RaPa CoOCoB NumFa

Jumps

$$40 - 28 = 12$$

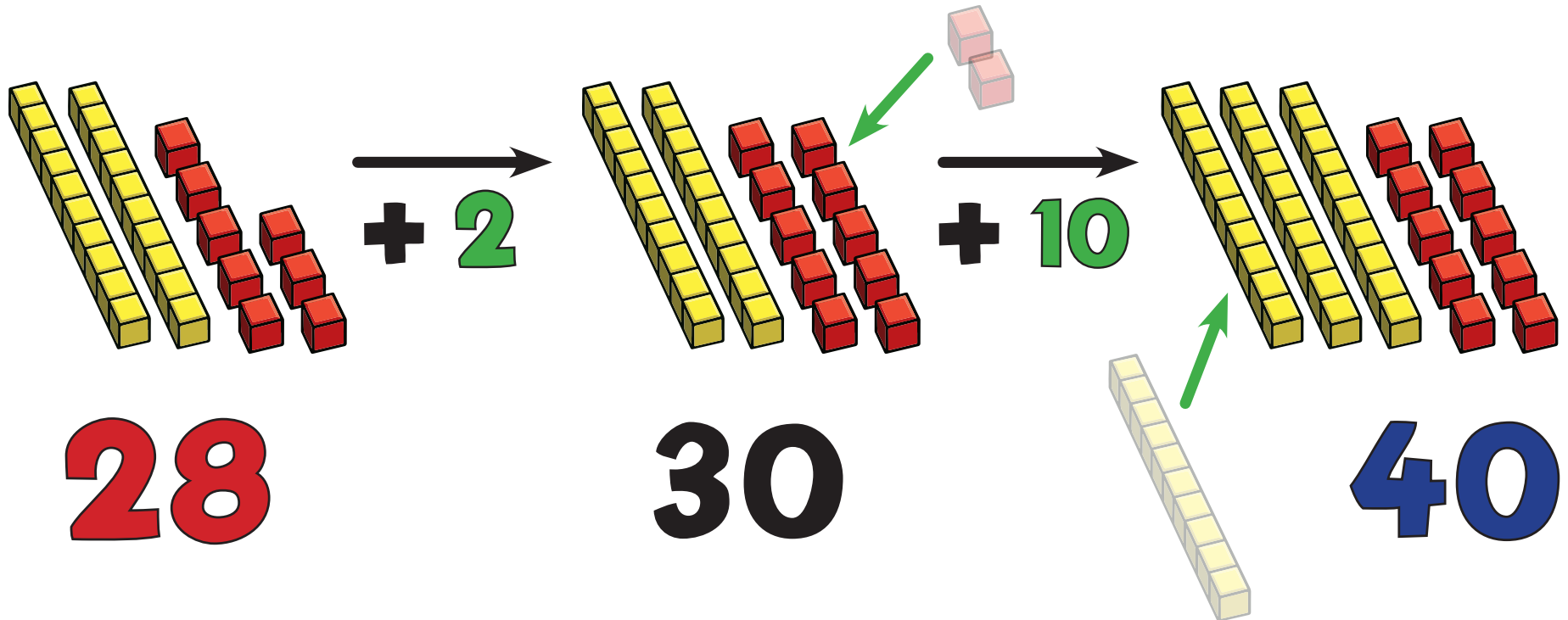


MS4b: Counting On

MC RaPa CoOCoB NumFa
Visualisation

Jumps

$$40 - 28 = 12$$



MS4b: Counting On

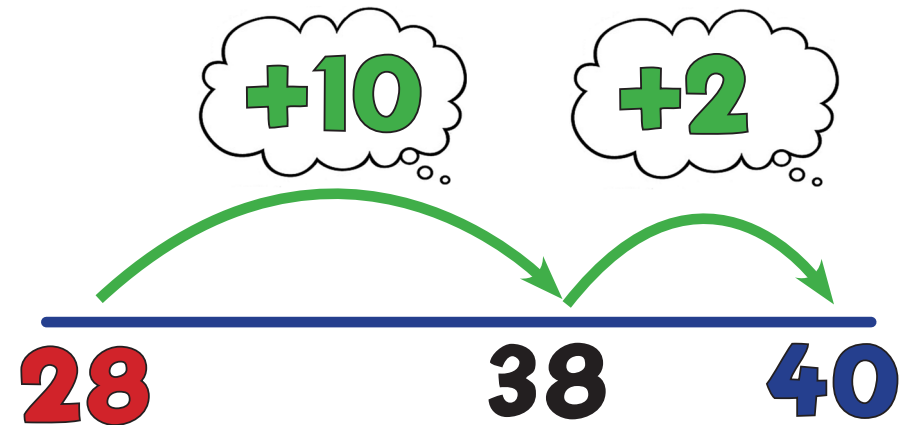
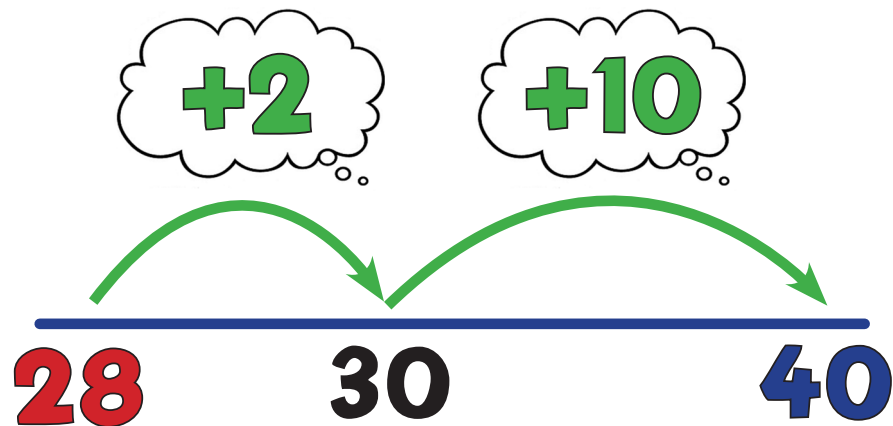


MC RaPa CoOCoB NumFa

2

Jumps

$$40 - 28 = 12$$



MS4b: Counting On

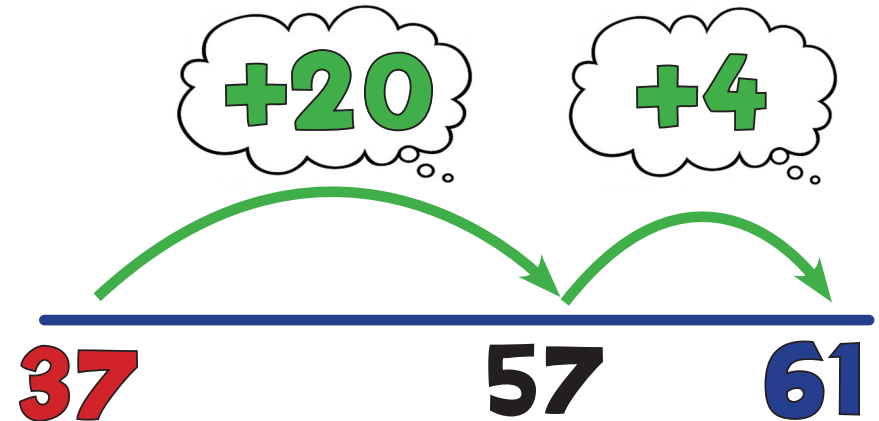
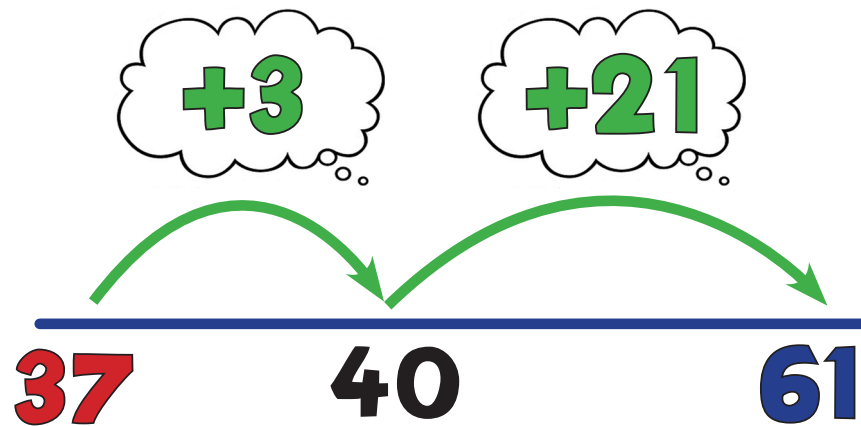


MC RaPa Co0CoB NumFa

3

Jumps

$$61 - 37 = 24$$



MS4b: Counting On



MC RaPa CoOCoB NumFa

4

Jumps

$$324 - 280 = 44$$

+20

+24



MS4b: Counting On



MC RaPa Co0CoB NumFa

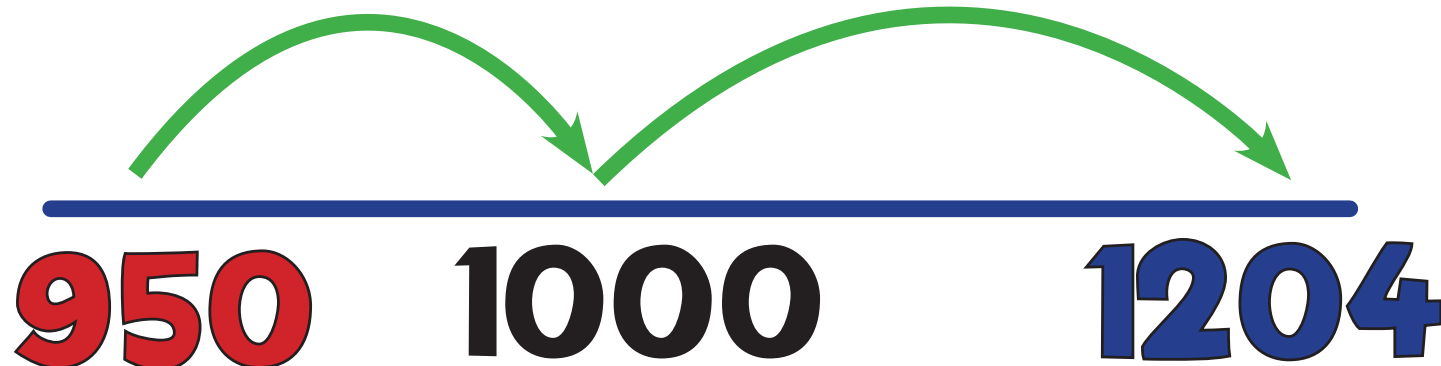
5

Jumps

$$1204 - 950 = 254$$

+50

+204



MS4b: Counting On



MC RaPa Co0CoB NumFa

6

Jumps

$$12.4 - 9.8 = 2.6$$

+0.2

+2.4

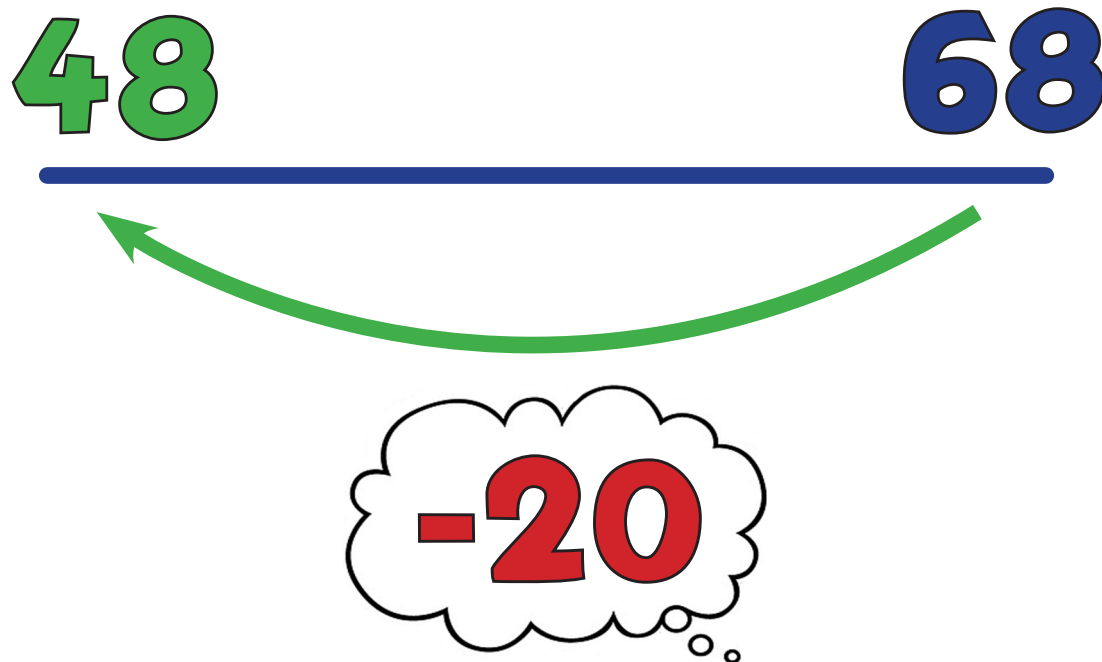


MS5a: Counting Back



MC RaPa CoOCoB NumFa

$$68 - 20 = 48$$

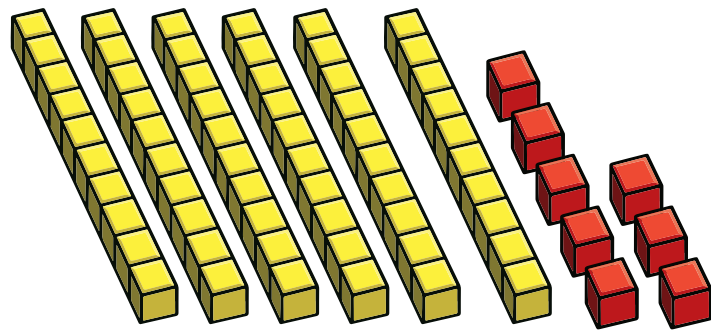


MS5a: Counting Back



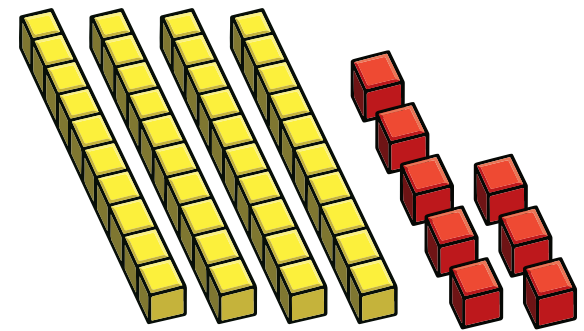
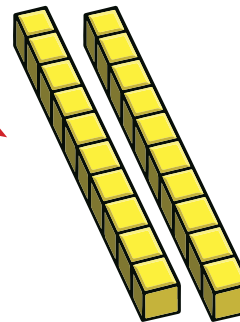
MC RaPa CoOCob NumFa
Visualisation

$$68 - 20 = 48$$



68

-20



48



MS5a: Counting Back



MC RaPa CoOCoB NumFa

1

$$15 - 4 = 11$$



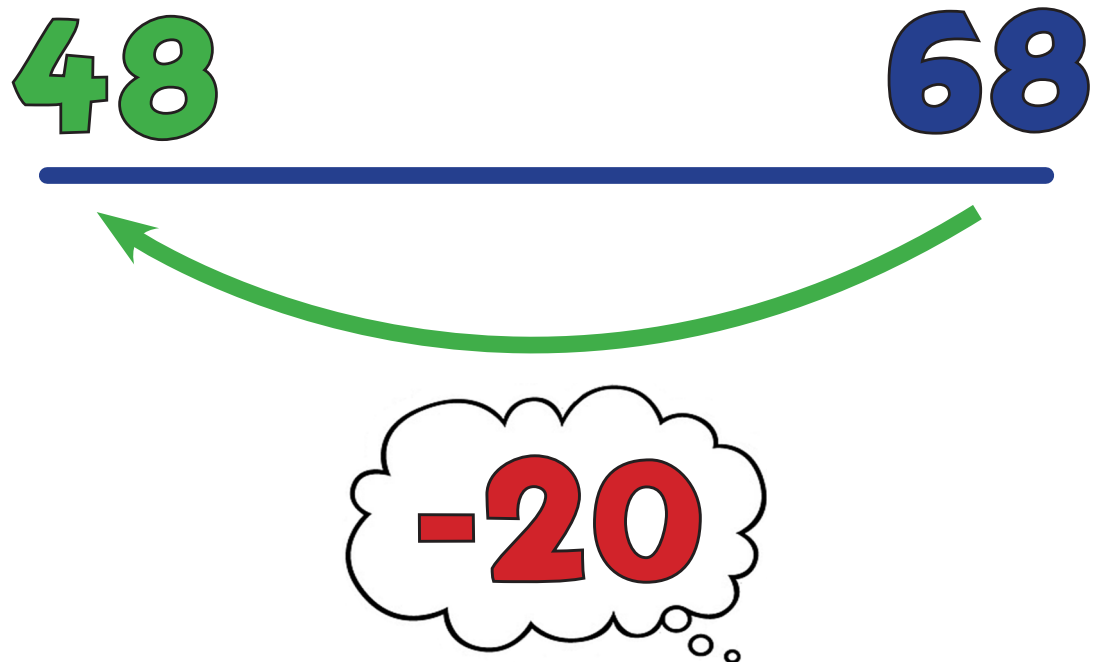
MS5a: Counting Back



MC RaPa CoOCoB NumFa

2

$$68 - 20 = 48$$



MS5a: Counting Back



MC RaPa CoOCoB NumFa

3

$$378 - 50 = 328$$

328

378



MS5a: Counting Back



MC RaPa CoOCoB NumFa

4

$$768 - 200 = 568$$

568

768



-200



MS5a: Counting Back



MC RaPa CoOCoB NumFa

5

$$7291 - 2000 = 5291$$

5291

7291



-2000



MS5a: Counting Back

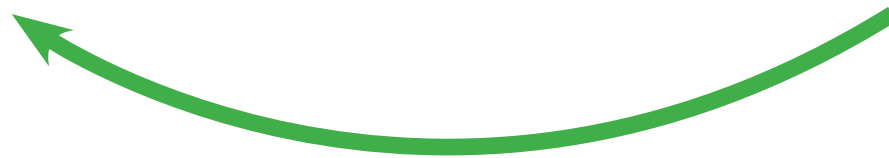


MC RaPa CoOCoB NumFa

6

$$86374 - 20000 = 66374$$

66374 86374



-20000



MS5b: Counting Back



MC RaPa CoOCoB NumFa

Jumps

$$86 - 12 = 74$$

$$- 10 - 2$$

86

76

74



MS5b: Counting Back

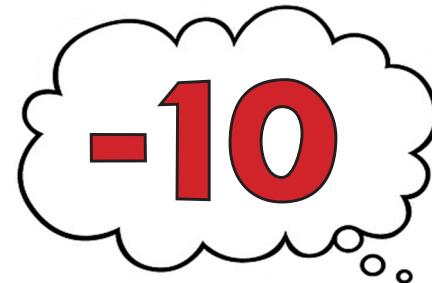
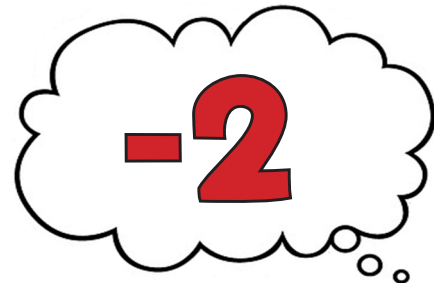


MC RaPa CoOCoB NumFa
Visualisation

Jumps

$$86 - 12 = 74$$

74 76 86



MS5b: Counting Back



MC RaPa CoOCoB NumFa

2

Jumps

$$86 - 12 = 74$$

$$- 10 - 2$$

86

76

74



MS5b: Counting Back



MC RaPa CoOCoB NumFa

3

Jumps

$$89 - 34 = 55$$

$$- 30 - 4$$

89

59

55



MS5b: Counting Back



MC RaPa CoOCoB NumFa

4

Jumps

$$578 - 45 = 533$$

$$- 40 - 5$$

578

538

533



MS5b: Counting Back



MC RaPa CoOCoB NumFa

5

Jumps

$$8.6 - 4.1 = 4.5$$

- 4 - 0.1

8.6

4.6

4.5



MS5b: Counting Back



MC RaPa CoOCoB NumFa

6

Jumps

$$\text{€}65.87 - \text{€}30.24 = \text{€}35.63$$

$-\text{€}30 \quad -24\text{p}$

€65.87

€35.87

€35.63



MS6: Number Facts



MC RaPa CoOCoB NumFa

$$61 - 41 = 20$$


$$41 + 20 = 61$$



MS6: Number Facts



MC RaPa CoOCoB NumFa
Visualisation

$$61 - 41 = 20$$

$$41 + 20 = 61$$

40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	
	Orange bar											Orange bar																			



MS6: Number Facts



MC RaPa CoOCoB NumFa

1

$$19 - 9 = 10$$

$$9 + 10 = 19$$



MS6: Number Facts



MC RaPa CoOCoB NumFa

2

$$61 - 41 = 20$$

$$41 + 20 = 61$$



MS6: Number Facts



MC RaPa CoOCoB NumFa

3

$$123 - 83 = 40$$


$$83 + 40 = 123$$



MS6: Number Facts



MC RaPa CoOCoB NumFa

4

$$847 - 447 = 400$$

$$447 + 400 = 847$$



MS6: Number Facts



MC RaPa CoOCoB NumFa

5

$$1424 - 724 = 700$$

$$724 + 700 = 1424$$



MS6: Number Facts



MC RaPa CoOCoB NumFa

6

$$13.2 - 9.2 = 4$$

$$9.2 + 4 = 13.2$$



Mental Multiplication

132	MM1	Manipulate Calculation
139	MM2	Factorising
146	MM3	Re-ordering
149	MM4	Partitioning
154	MM5	Round & Adjust
158	MM6	Doubling
166	MM7	Doubling Table Facts
170	MM8	Doubling Up
173	MM9	Multiply by ... then Halve
175	MM10	Jump



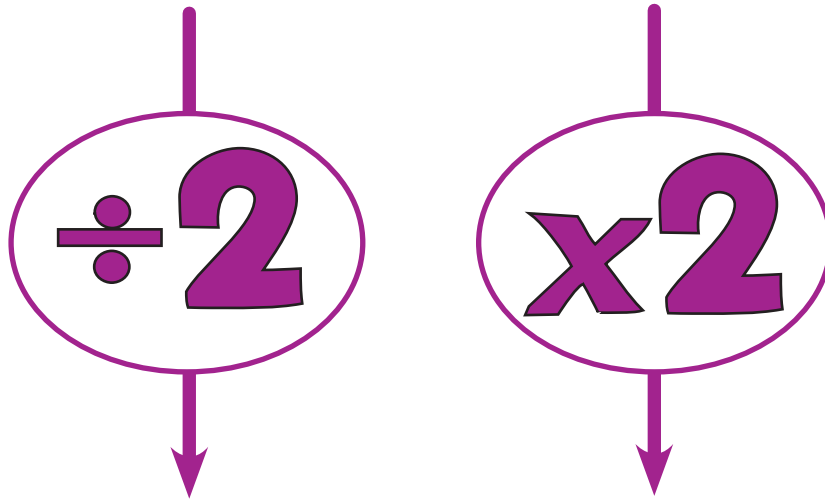
10 Cool Strategies for Mental Multiplication



MM1: Manipulate Calculation

5

$$16 \times 3$$



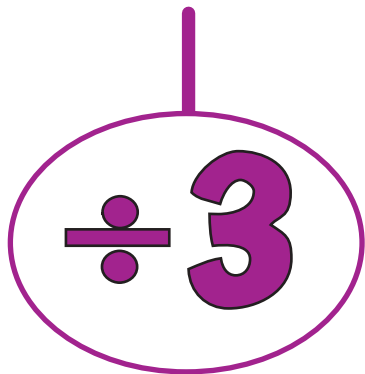
$$8 \times 6 = 48$$



MM1a: Manipulate Calculation

5

$$27 \times 3$$



$$9 \times 9 = 81$$



MM1b: Manipulate Calculation

5

$$45 \times 14$$



$$90 \times 7 = 630$$



MM1c: Manipulate Calculation

5/6

$$36 \times 25$$

A purple circle containing the expression $\div 4$. A vertical purple line connects the top of the circle to the number 36 in the equation above. A purple arrow points downwards from the bottom of the circle to the number 9 in the equation below.

A purple circle containing the expression $\times 4$. A vertical purple line connects the top of the circle to the number 25 in the equation above. A purple arrow points downwards from the bottom of the circle to the number 100 in the equation below.

$$9 \times 100 = 900$$



MM1d: Manipulate Calculation

6

$$32 \times 15$$



$$160 \times 3 = 480$$



MM1e: Manipulate Calculation

6

$$26 \times 32$$



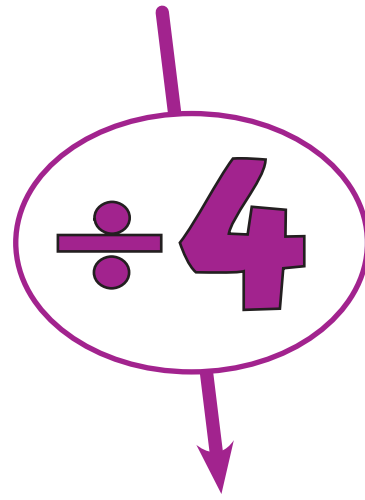
$$104 \times 8 = 832$$



MM1f: Manipulate Calculation

6

$$52 \times 24$$



$$208 \times 6 = 1248$$



MM2: Factorising

4

$$16 \times 3 = 48$$

$$(8 \times 2 \times 3)$$

$$8 \times 6 = 48$$



MM2a: Factorising

4

$$27 \times 3 = 81$$

$$(9 \times 3 \times 3)$$

$$9 \times 9 = 81$$



MM2b: Factorising

5

$$45 \times 14 = 630$$

$$(45 \times 2 \times 7)$$

$$90 \times 7 = 630$$



MM2c: Factorising

5/6

$$36 \times 25 = 900$$

$$(9 \times 4 \times 25)$$

$$9 \times 100 = 900$$



MM2d: Factorising

6

$$32 \times 15 = 480$$

$$(32 \times 5 \times 3)$$

$$160 \times 3 = 480$$



MM2e: Factorising

6

$$26 \times 32 = 832$$

$$(26 \times 4 \times 8)$$

$$104 \times 8 = 832$$



MM2f: Factorising

6

$$52 \times 24 = 1248$$

$$(52 \times 4 \times 6)$$

$$208 \times 6 = 1248$$



MM3: Re-ordering

5

$$(9 \times 2) \times 5$$
$$18 \times 5 = 90$$

$$(9 \times 5) \times 2$$
$$45 \times 2 = 90$$

$$(2 \times 5) \times 9$$
$$10 \times 9 = 90 \quad *$$



MM3a: Re-ordering

5/6

$$(7 \times 4) \times 5$$

$$28 \times 5 = 140$$

$$(7 \times 5) \times 4$$

$$35 \times 4 = 140$$

$$(4 \times 5) \times 7$$

$$20 \times 7 = 140 *$$



MM3b: Re-ordering

6

$$(9 \times 8) \times 6$$

$$72 \times 6 = 432$$

$$(9 \times 6) \times 8$$

$$54 \times 8 = 432 *$$

$$(8 \times 6) \times 9$$

$$48 \times 9 = 432$$



MM4: Partitioning

4

$$15 \times 5 = 75$$

$$\begin{array}{c} \text{50} \\ \text{(10 x 5)} \end{array} + \begin{array}{c} \text{25} \\ \text{(5 x 5)} \end{array} = 75$$



MM4a: Partitioning

4/5

$$37 \times 4 = 148$$

$$\begin{array}{c} \text{120} \\ \text{(30 x 4)} \end{array} + \begin{array}{c} \text{28} \\ \text{(7 x 4)} \end{array} = 148$$



MM4b: Partitioning

5

$$126 \times 6 = 756$$

$$\begin{array}{c} \text{600} \\ \text{(100 x 6)} \end{array} + \begin{array}{c} \text{120} \\ \text{(20 x 6)} \end{array} + \begin{array}{c} \text{36} \\ \text{(6 x 6)} \end{array} = 756$$



MM4c: Partitioning

6

$$4.3 \times 8 = 34.4$$

$$\begin{array}{c} \text{32} \\ (4 \times 8) \end{array} + \begin{array}{c} \text{2.4} \\ (0.3 \times 8) \end{array} = 34.4$$



MM4d: Partitioning

6

$$2.16 \times 3 = 6.48$$

$$\begin{array}{c} \text{6} \\ \text{(2 x 3)} \end{array} + \begin{array}{c} \text{0.3} \\ \text{(0.1 x 3)} \end{array} + \begin{array}{c} \text{0.18} \\ \text{(0.06 x 3)} \end{array} = 6.48$$



MM5: Round & Adjust

4

$$49 \times 3 = 147$$

$$(50 \times 3) - (1 \times 3)$$

$$150 - 3 = 147$$



MM5a: Round & Adjust

5

$$198 \times 4 = 792$$

$$(200 \times 4) - (2 \times 4)$$

$$800 - 8 = 792$$



MM5b: Round & Adjust

5/6

$$3.9 \times 5 = 19.5$$

$$(4 \times 5) - (0.1 \times 5)$$

$$20 - 0.5 = 19.5$$



MM5c: Round & Adjust

6

$$\text{€}5.99 \times 6 = \text{€}35.94$$

$$(\text{€}6 \times 6) - (1\text{p} \times 6)$$

$$\text{€}36 - 6\text{p} = \text{€}35.94$$



MM6: Doubling

2

$$20 + 14 = 34$$

Double $17 = 34$

(15 + 2)

$$30 + 4 = 34$$



MM6a: Doubling

3

$$60 + 14 = 74$$

$$\text{Double } 37 = 74$$

(35 + 2)

$$70 + 4 = 74$$



MM6b: Doubling

4

$$140 + 16 = 156$$

$$\text{Double } 78 = 156$$

(75 + 3)

$$150 + 6 = 156$$



MM6c: Doubling

4

$$\text{Double } 340 = 680$$

A diagram illustrating the doubling of 340. A blue diagonal line connects the '3' in 340 to the '6' in 600. A red diagonal line connects the '40' in 340 to the '80' in 80. This shows that 340 is split into 300 and 40, which are then doubled to 600 and 80.

$$600 + 80 = 680$$



MM6d: Doubling

4/5

$$800 + 160 = 960$$

$$\text{Double } 480 = 960$$

(450 + 30)

$$900 + 60 = 960$$



MM6e: Doubling

5

$$400 + 140 + 16 = 556$$

$$\text{Double } 278 = 556$$

(250 + 28)

$$500 + 28 = 556$$



MM6f: Doubling

5/6

$$1400 + 120 + 16 = 1536$$


$$\text{Double } 768 = 1536$$

(750 + 18)



$$1500 + 36 = 1536$$



MM6g: Doubling

6

$$\text{Double } 3.7 = 7.4$$


$$6 + 1.4 = 7.4$$



MM7: Doubling Table Facts

3

$$8 \times 6 = 48$$

(4 x 2)

$$4 \times 6 = 24$$



$$8 \times 6 = 48$$



x 2



MM7a: Doubling Table Facts

4

$$12 \times 7 = 84$$

(6 x 2)

$$\begin{array}{ccc} 6 \times 7 = 42 & & \\ \downarrow & & \downarrow \times 2 \\ 12 \times 7 = 84 & & \end{array}$$



MM7b: Doubling Table Facts

5

$$16 \times 7 = 112$$

(8 x 2)

$$8 \times 7 = 56$$

↓

$$16 \times 7 = 112$$

↓ x 2



MM7c: Doubling Table Facts

6

$$\begin{array}{l} 22 \times 12 = 264 \\ (11 \times 2) \end{array}$$

$$\begin{array}{l} 11 \times 12 = 132 \\ \downarrow \qquad \qquad \qquad \downarrow \times 2 \\ 22 \times 12 = 264 \end{array}$$



MM8: Doubling Up

3/4

$$17 \times 4 = 68$$

$$\text{Double } 17 = 34 \quad (17 \times 2)$$

$$\text{Double } 34 = 68 \quad (17 \times 4)$$



MM8a: Doubling Up

5

$$36 \times 8 = 288$$

$$\text{Double } 36 = 72 \quad (36 \times 2)$$

$$\text{Double } 72 = 144 \quad (36 \times 4)$$

$$\text{Double } 144 = 288 \quad (36 \times 8)$$



MM8b: Doubling Up

6

$$125 \times 16 = 2000$$

$$\text{Double } 125 = 250 \quad (125 \times 2)$$

$$\text{Double } 250 = 500 \quad (125 \times 4)$$

$$\text{Double } 500 = 1000 \quad (125 \times 8)$$

$$\text{Double } 1000 = 2000 \quad (125 \times 16)$$



MM9: Mult by ^{10, 100}_{& 1000} then Halve

5

$$86 \times 5 = 430$$

$$86 \times 10 = 860$$

$$860 \div 2 = 430$$



MM9a: Mult by ^{10, 100} & ¹⁰⁰⁰ then Halve

6

$$56 \times 25 = 1400$$

$$56 \times 100 = 5600$$

$$5600 \div 2 = 2800$$

$$2800 \div 2 = 1400$$



MM10: Jump!

3/4

x100

x10

1000 100 10 1

3400

340

34



MM10a: Jump!

5/6

x1000

x100

x10

634000

6340

634

63.4



Mental Division

- 178 **MD1** Manipulate Calculation
- 185 **MD2** Divide by 100 then Double
- 187 **MD3** Halving
- 194 **MD4** Halve and Halve Again
- 198 **MD5** Division as a Fraction
- 205 **MD6** Find the Hunk
- 211 **MD7** Jump



7 Cool Strategies for Mental Division!



MD1: Manipulate Calculation

3

Small Quotient

$$140 \div 20$$

↓

$$\div 10$$

↓

↓

$$\div 10$$

↓

$$14 \div 2 = 7$$



MD1a: Manipulate Calculation

4

Small Quotient

$$84 \div 12$$

$$\div 2$$

$$\div 2$$

$$42 \div 6 = 7$$

$$\div 2$$

$$\div 2$$

$$21 \div 3 = 7$$

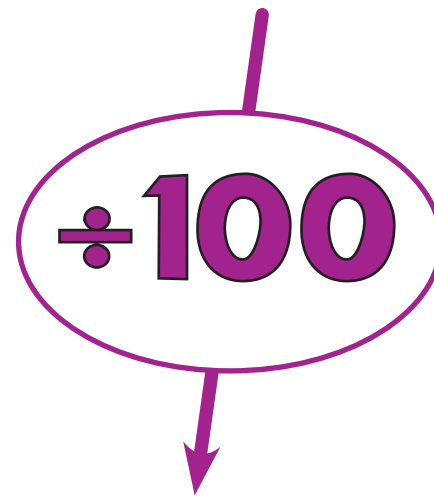
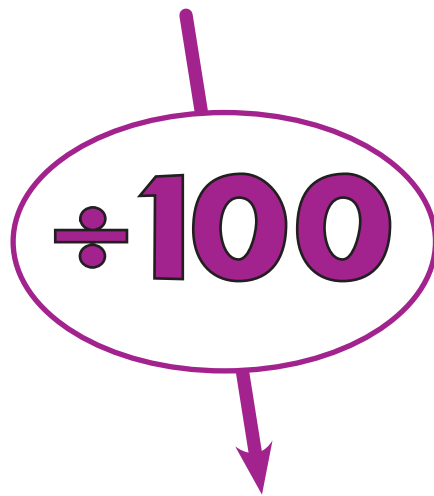


MD1b: Manipulate Calculation

4

Small Quotient

$$1200 \div 400$$



$$12 \div 4 = 3$$



MD1c: Manipulate Calculation

5

Small Quotient

$$162 \div 18$$

$\div 2$

$\div 2$

$$81 \div 9 = 9$$

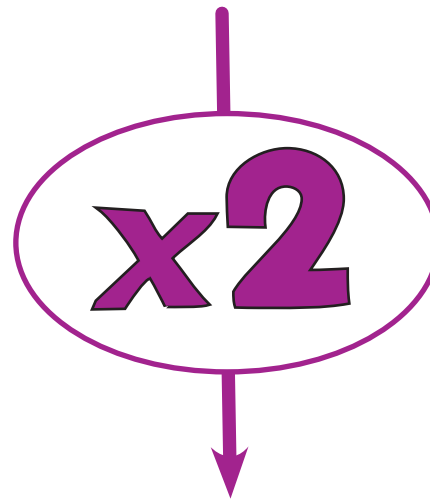
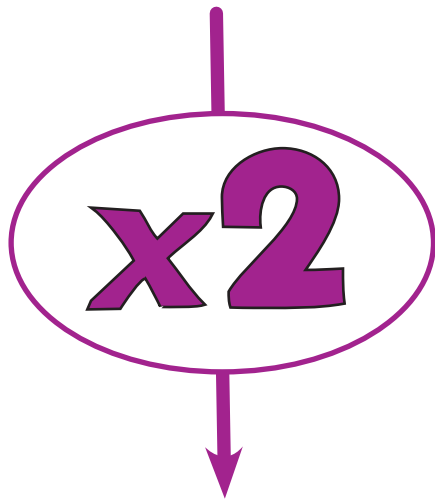


MD1d: Manipulate Calculation

6

Small Quotient

$$18 \div 1.5$$



$$36 \div 3 = 12$$

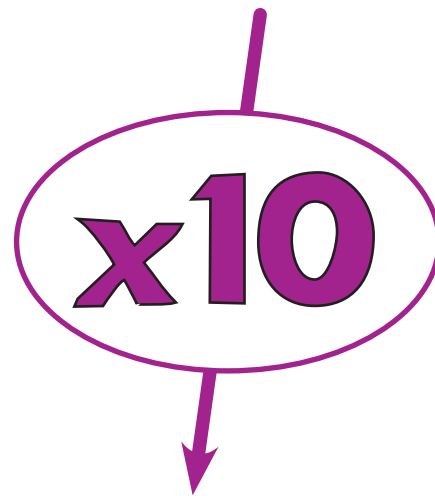
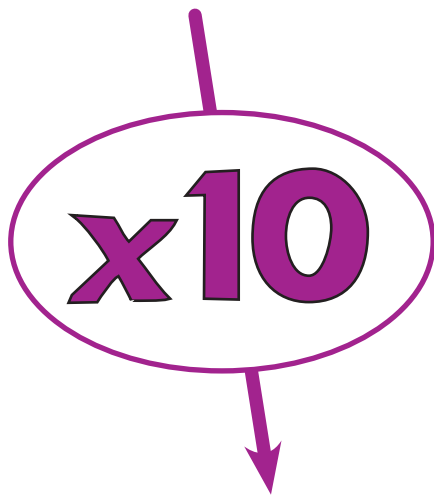


MD1e: Manipulate Calculation

6

Small Quotient

$$9.3 \div 0.3$$



$$93 \div 3 = 31$$

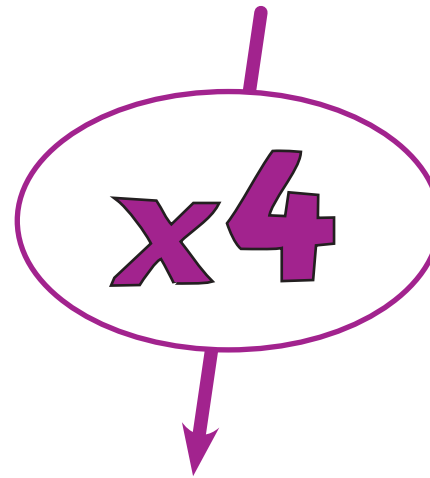
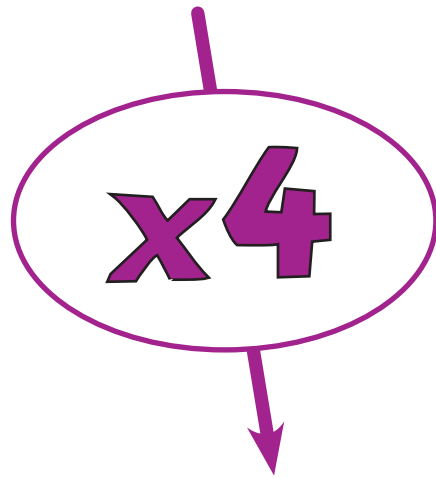


MD1f: Manipulate Calculation

6

Small Quotient

$$6.25 \div 0.25$$



$$25 \div 1 = 25$$



MD2: Divide by 100 then Double

4

$$800 \div 50 = 16$$

$$800 \div 100 = 8$$

$$8 \times 2 = 16$$



MD2a: Divide by 100 then Double twice

5

$$8000 \div 25 = 320$$

$$8000 \div 100 = 80$$

$$80 \times 2 = 160$$

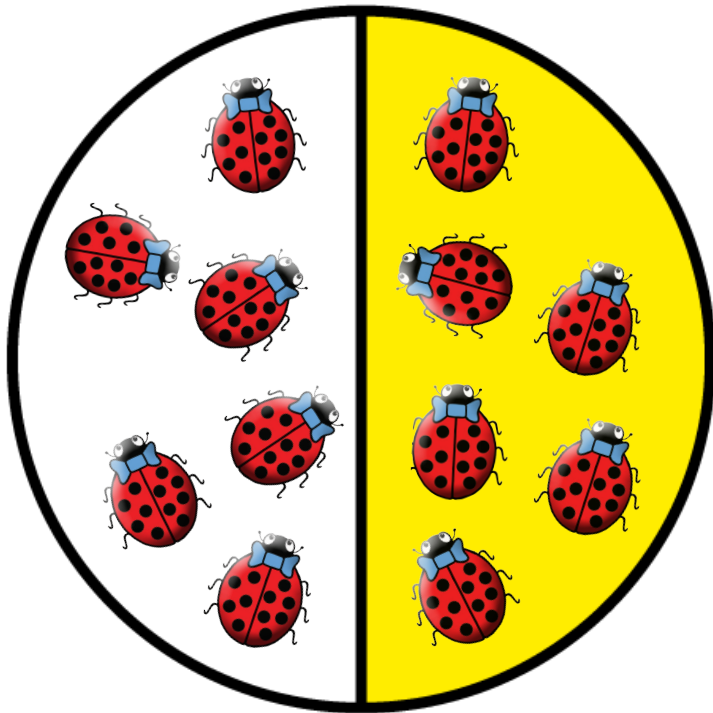
$$160 \times 2 = 320$$



MD3: Halving

1

Half of 12 is equivalent to $12 \div 2$



$$\frac{1}{2} \text{ of } 12 = 12 \div 2$$



MD3a: Halving

2

Half of ⁽²⁰⁾ 26

$$10 + 3 = 13$$



MD3b: Halving

3

Half of ⁽⁵⁰⁾58

$$25 + 4 = 29$$



MD3c: Halving

4

Half of 92 ^(80 + 12)

40 + 6 = 46

Half of 92

45 + 1 = 46



MD3d: Halving

5

Half of **326** ^(32 tens)

$$160 + 3 = 163$$

Half of **326**

$$150 + 10 + 3 = 163$$



MD3e: Halving

6

Half of 5.84

A diagram illustrating the halving of 5.84. Three arrows point from the digits of 5.84 to the components of the sum below: 2.5 (from 5), 0.4 (from 8), and 0.02 (from 4). The sum is shown as 2.5 + 0.4 + 0.02 = 2.92.

$$2.5 + 0.4 + 0.02 = 2.92$$



MD3f: Halving

6

$$\text{Half of } 34.72 = 17.36$$

$$15 + 2 + 0.35 + 0.01$$

(2 tens + 14 ones + 6 tenths + 12 hundredths)

$$\text{Half of } 34.72$$

$$10 + 7 + 0.3 + 0.06$$



MD4: Halve & Halve Again

3

$$84 \div 4 = 21$$

$$\text{Half of } 84 = 42 \quad (84 \div 2)$$

$$\text{Half of } 42 = 21 \quad (84 \div 4)$$



MD4a: Halve & Halve Again

4 (finding a quarter)

$$128 \div 4 = 32$$

$$\text{Half of } 128 = 64 \quad (128 \div 2)$$

$$\text{Half of } 64 = 32 \quad (128 \div 4)$$



MD4b: Halve, Halve, Halve

5
(finding an eighth)

$$360 \div 8 = 45$$

$$\text{Half of } 360 = 180 \quad (360 \div 2)$$

$$\text{Half of } 180 = 90 \quad (360 \div 4)$$

$$\text{Half of } 90 = 45 \quad (360 \div 8)$$



MD4c: Halve, Halve, Halve

$$5000 \div 8 = 625$$

$$\text{Half of } 5000 = 2500 \quad (5000 \div 2)$$

$$\text{Half of } 2500 = 1250 \quad (5000 \div 4)$$

$$\text{Half of } 1250 = 625 \quad (5000 \div 8)$$

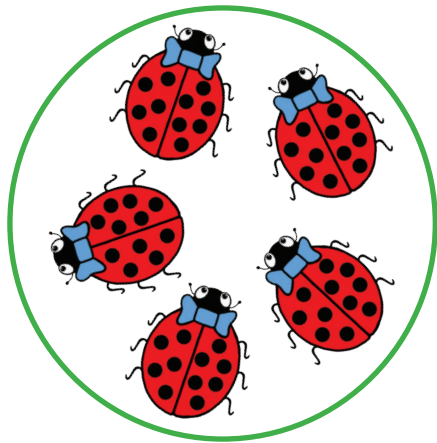


MD5: Division as a Fraction

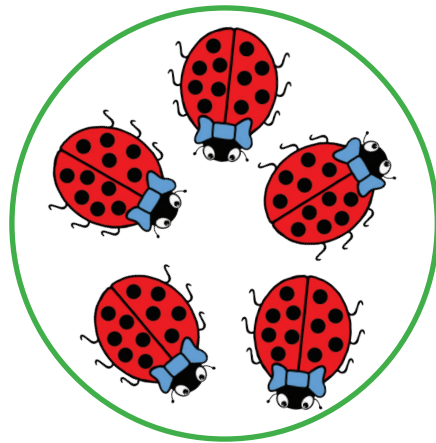
3

Sharing Model

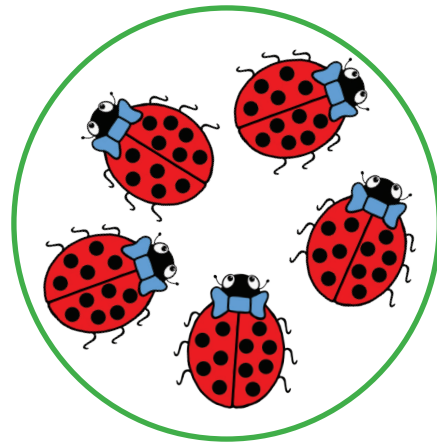
$$\frac{1}{4} \text{ of } 20 = 20 \div 4 = 5$$



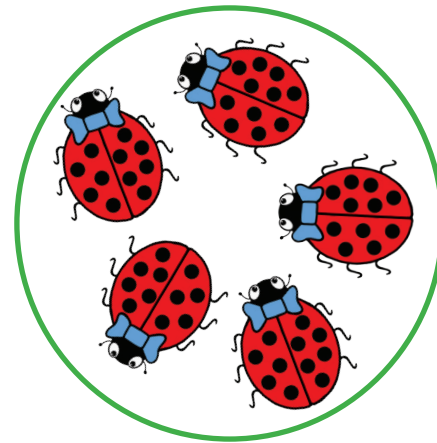
$\frac{1}{4}$



$\frac{1}{4}$



$\frac{1}{4}$



$\frac{1}{4}$

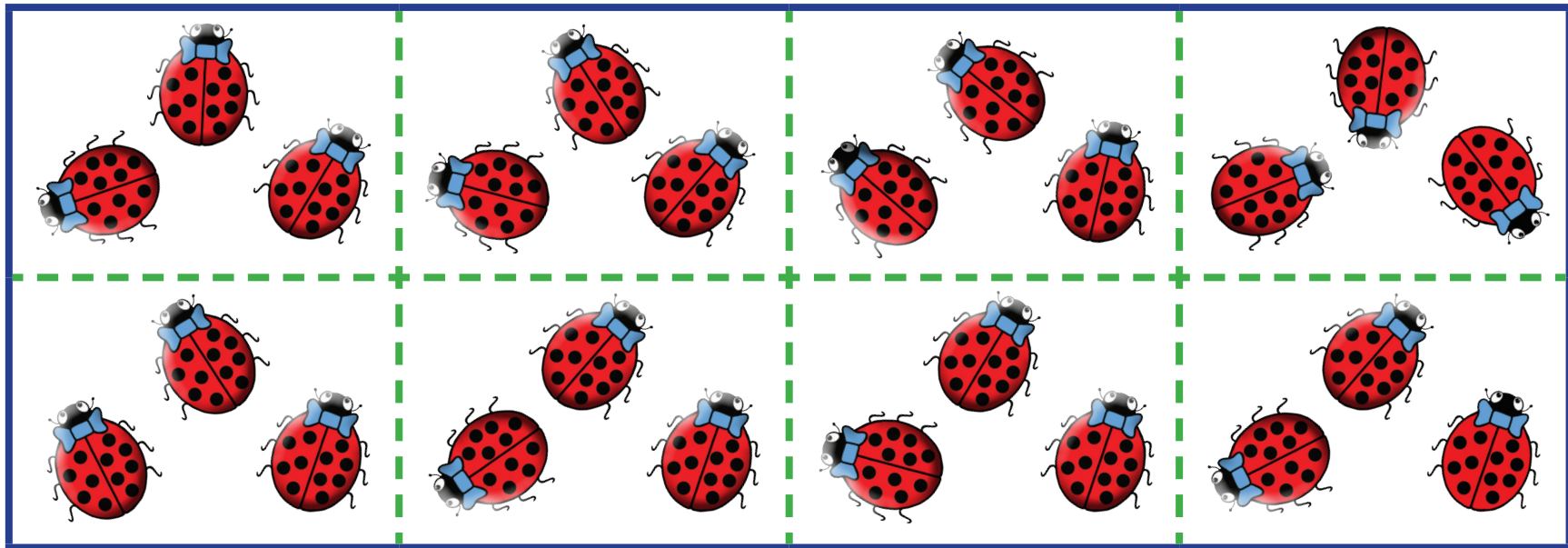


MD5a: Division as a Fraction

4

Sharing Model

$$\frac{1}{8} \text{ of } 24 = 24 \div 8 = 3$$



MD5b: Division as a Fraction

4

$$\frac{1}{4} \text{ of } 3 = 3 \div 4 = \frac{3}{4}$$

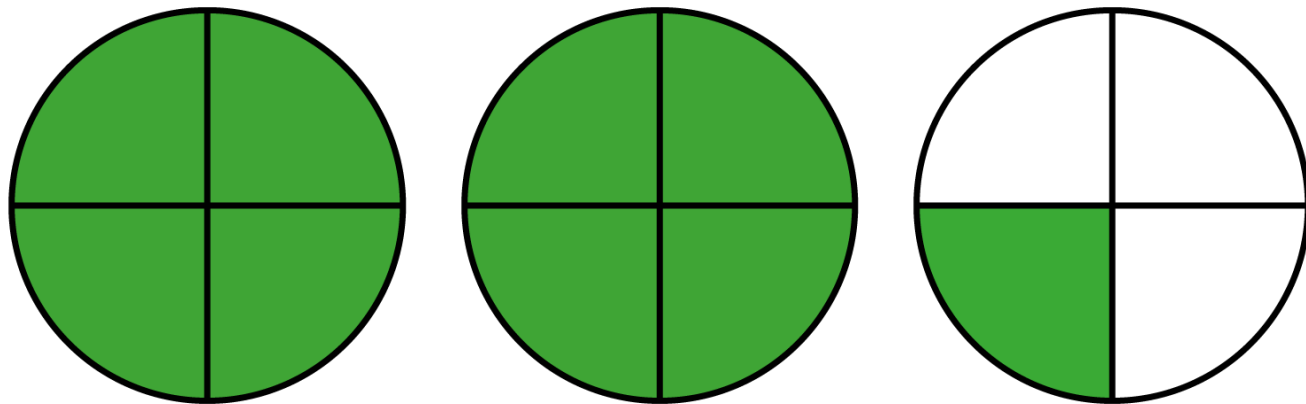


MD5c: Division as a Fraction

5

Mixed Number Model

$$\frac{1}{4} \text{ of } 9 = 9 \div 4 = \frac{9}{4} = 2\frac{1}{4}$$



(9 quarters = 2 and a quarter)



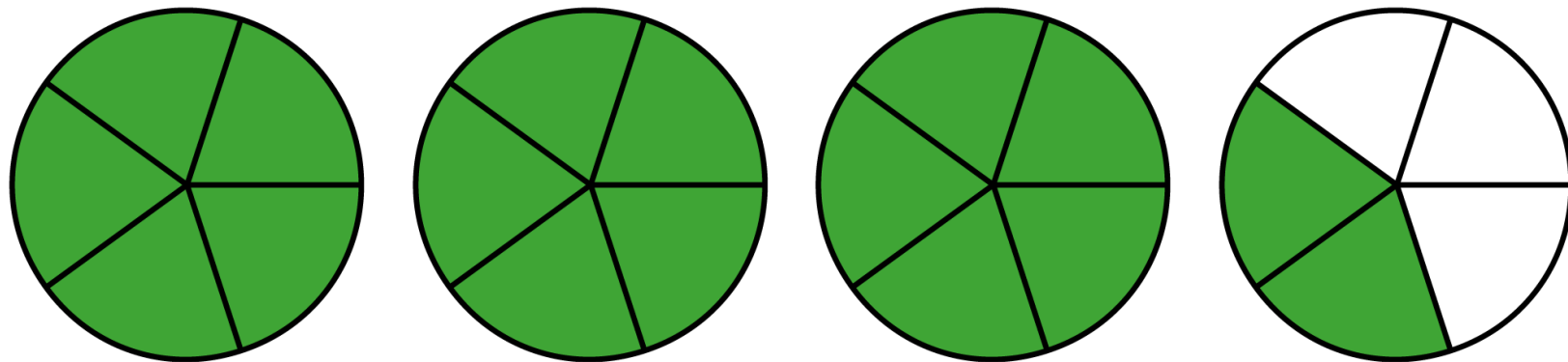
MD5d: Division as a Fraction

5

Mixed Number Model

$$\frac{1}{5} \text{ of } 17 = 17 \div 5 = \frac{17}{5} = 3 \frac{2}{5}$$

(3.4)



(17 fifths = 3 wholes and 2 fifths)



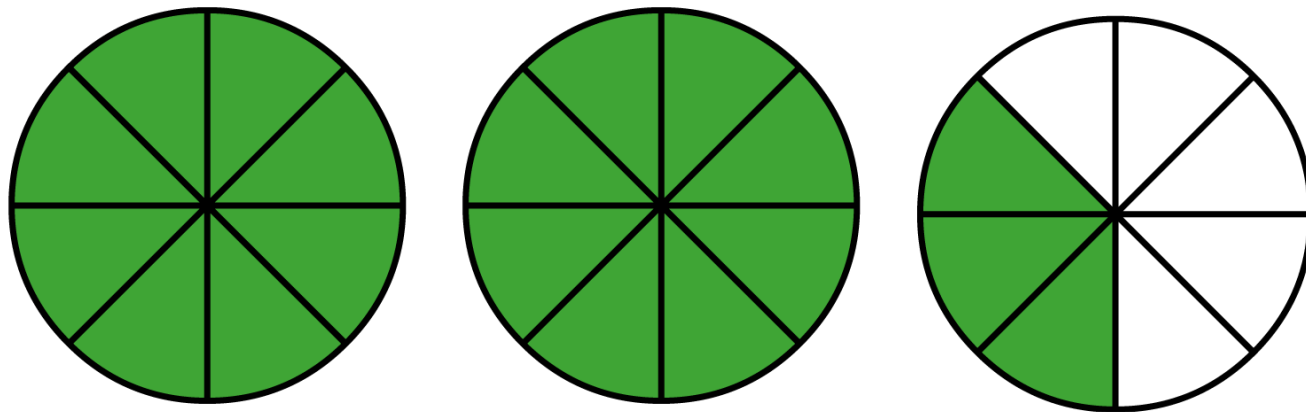
MD5e: Division as a Fraction

6

Mixed Number Model

$$\frac{1}{8} \text{ of } 19 = 19 \div 8 = \frac{19}{8} = 2\frac{3}{8}$$

(2.375)



(19 eighths = 2 and 3 eighths)

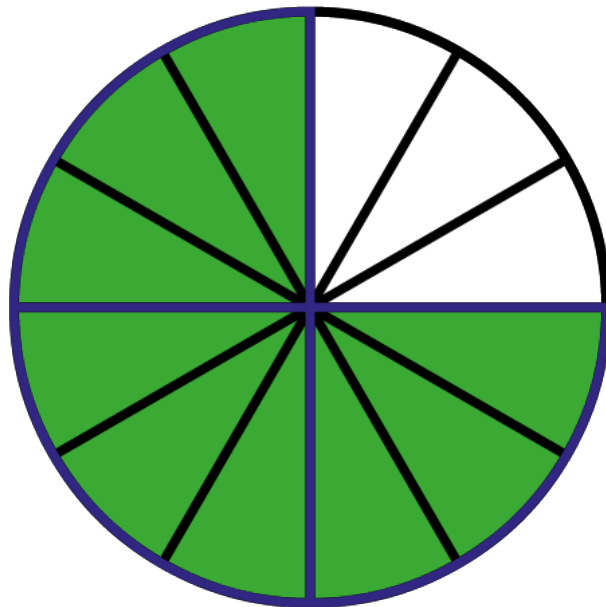


MD5f: Division as a Fraction

6

Mixed Number Model

$$\frac{1}{12} \text{ of } 9 = 9 \div 12 = \frac{9}{12} = \frac{3}{4} \quad (0.75)$$

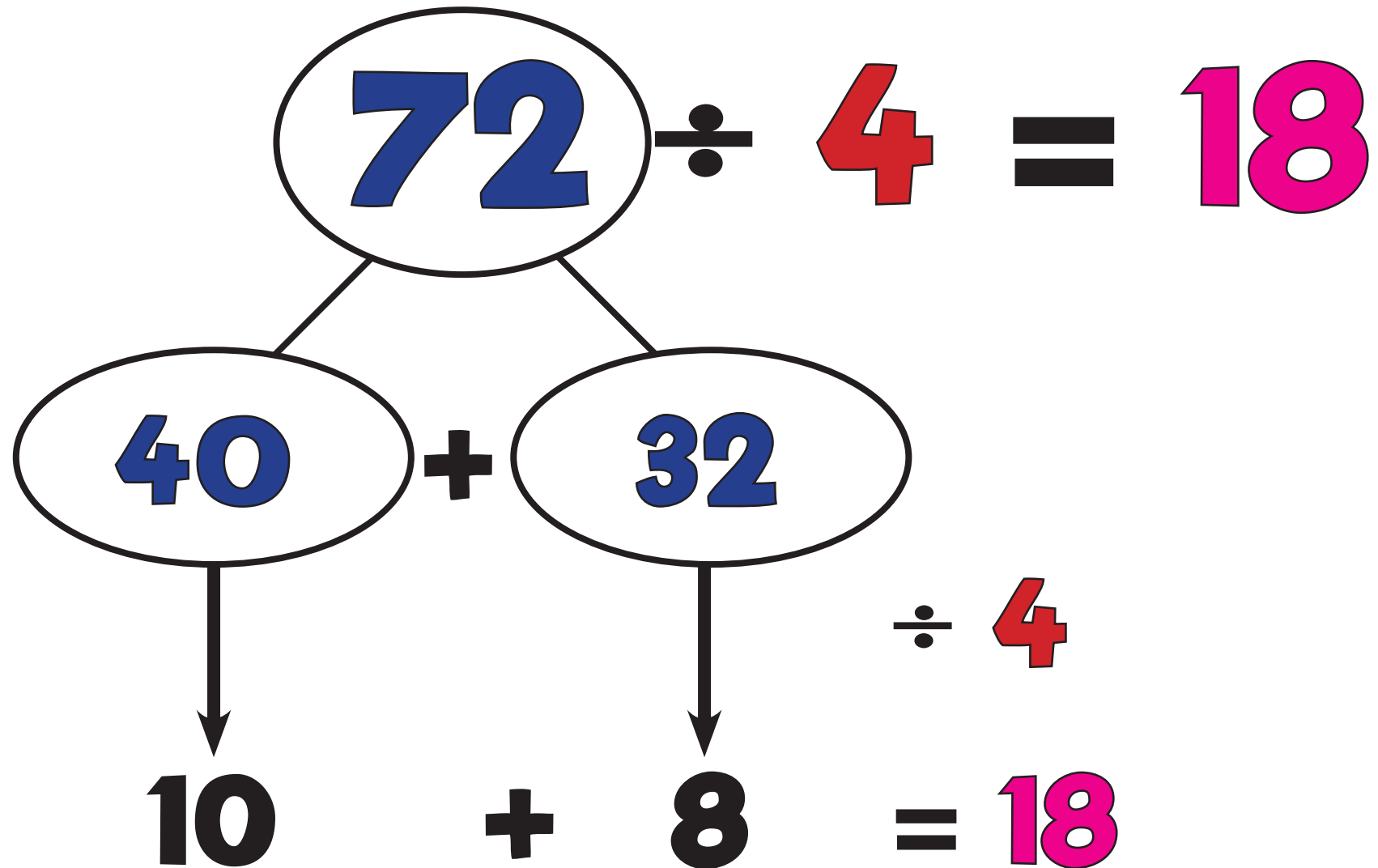


(9 twelfths =
3 quarters)



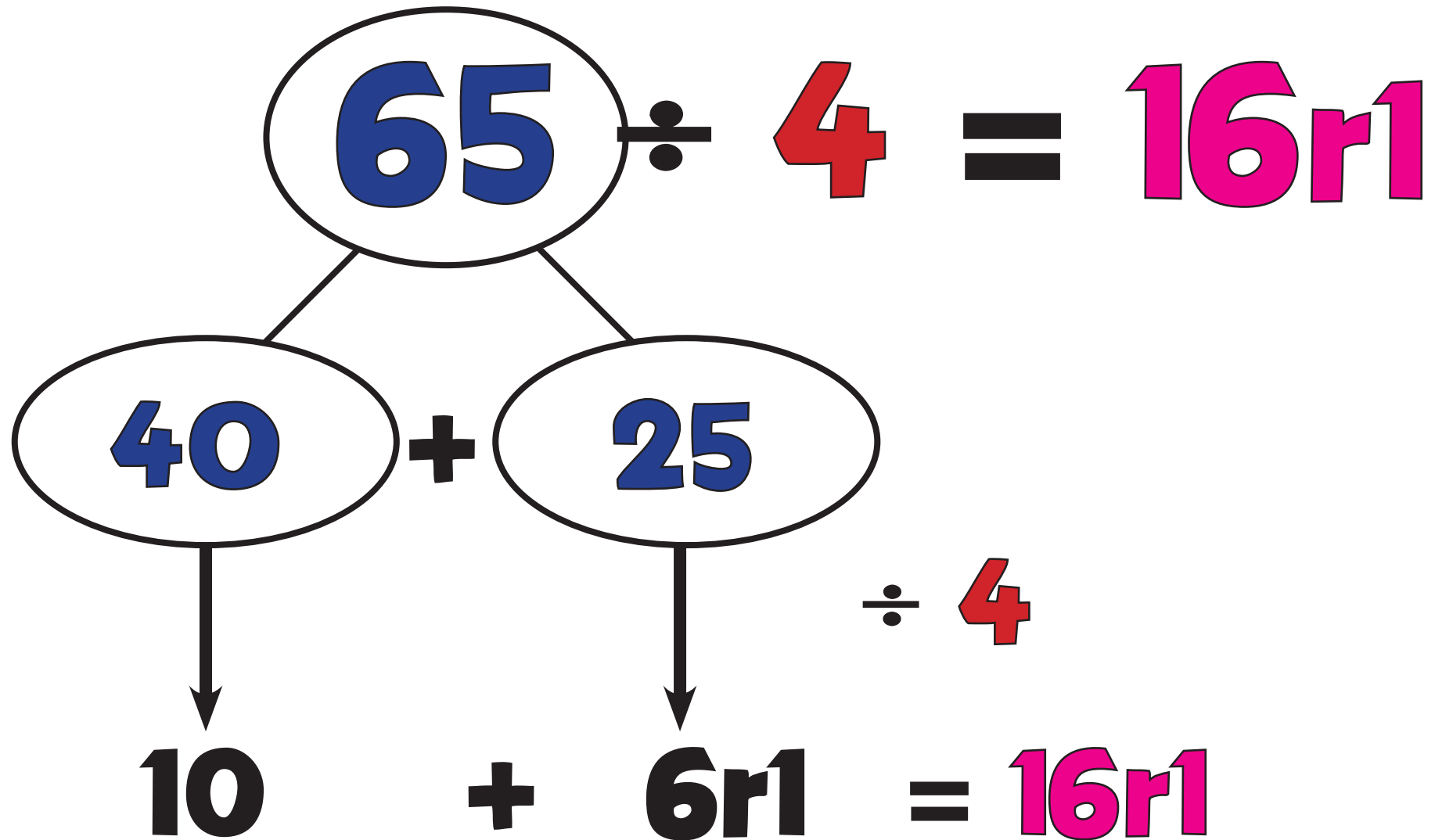
MD6: Find the Hunk!

4



MD6a: Find the Hunk!

4



MD6b: Find the Hunk!

5

$$136 \div 4 = 34$$

$$120 + 16$$

$$30 + 4 = 34$$



MD6c: Find the Hunk!

5

$$394 \div 6 = 65r4$$

$$360 + 34$$

$$60 + 5r4 = 65r4$$



MD6d: Find the Hunk!

5/6

$$\textcircled{536} \div 4 = 134$$

$$\textcircled{400} + \textcircled{120} + \textcircled{16}$$

$$100 + 30 + 4 = 134$$

$$\div 4$$



MD6e: Find the Hunk!

6

$$18 \div 1.5 = 12$$

$$\begin{array}{ccc} \textcircled{15} & + & \textcircled{3} \\ \downarrow & & \downarrow \\ 10 & + & 2 \end{array} \div 1.5 = 12$$



MD7: Jump ($\div 10$)

2

10 1

80

8



$\div 10$



MD7 a: Jump ($\div 10$)

3

100 10 1

360

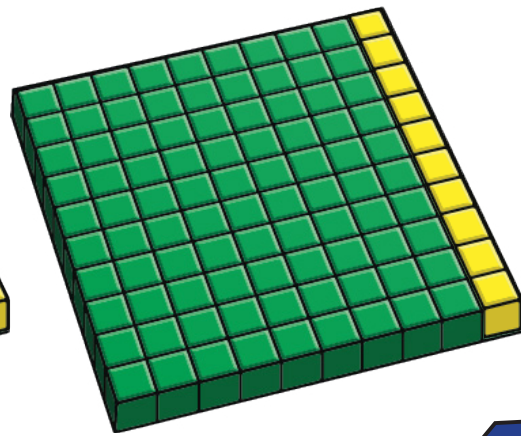
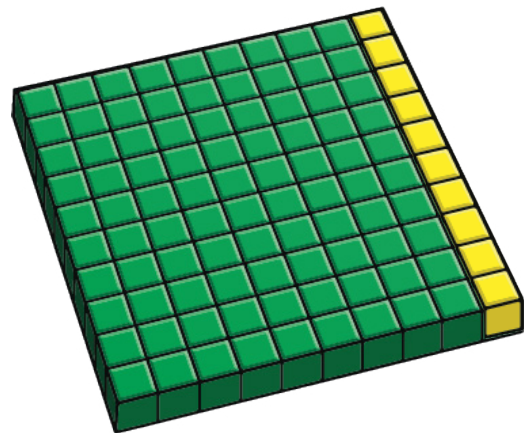
$\div 10$

36

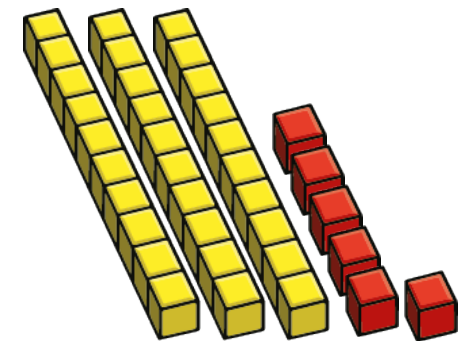
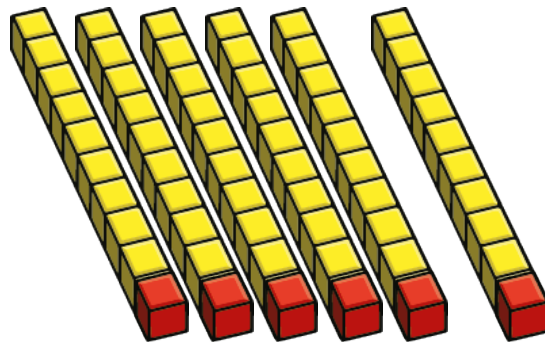
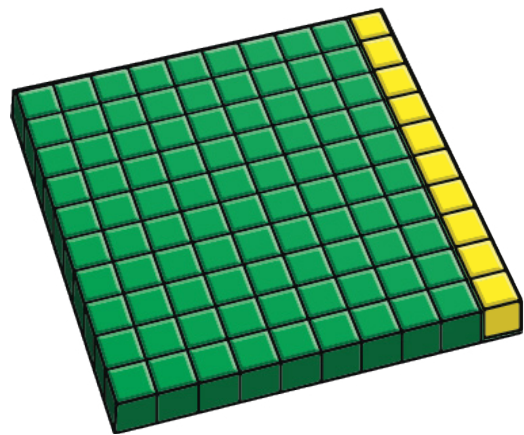


MD7a: Jump ($\div 10$)

3/4 (Pictorial)



$\div 10$



100 10 1

360

36

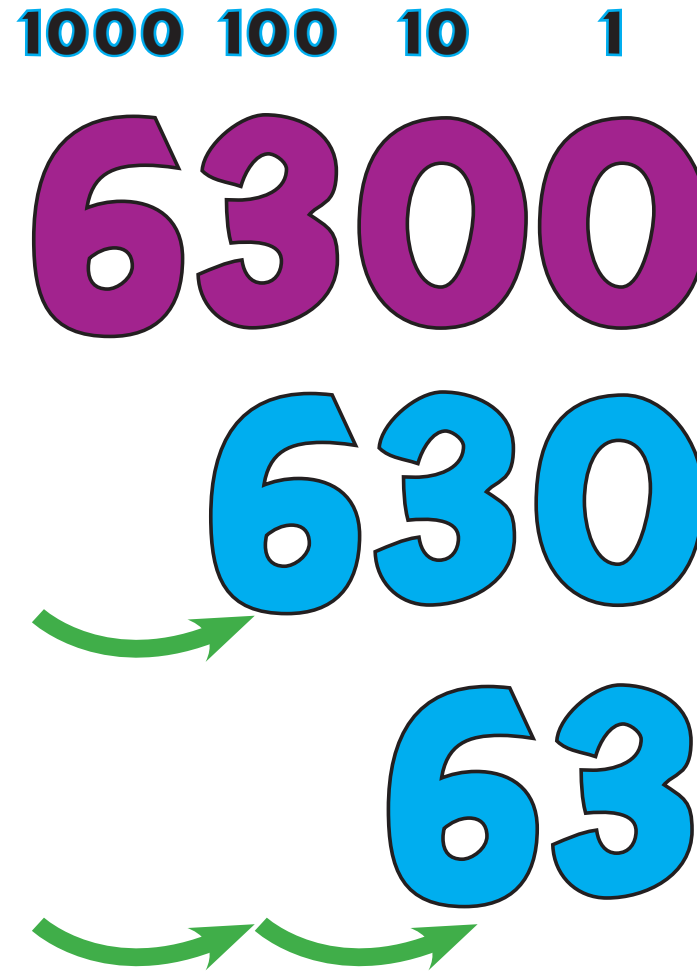


MD7b: Jump ($\div 10/100$)

4/5

$\div 10$

$\div 100$



MD7c: Jump ($\div 10/100/1000$)

5/6

100 10 1 ■ $\frac{1}{10}$ $\frac{1}{100}$ $\frac{1}{1000}$

634

$\div 10$

63.4

$\div 100$

6.34

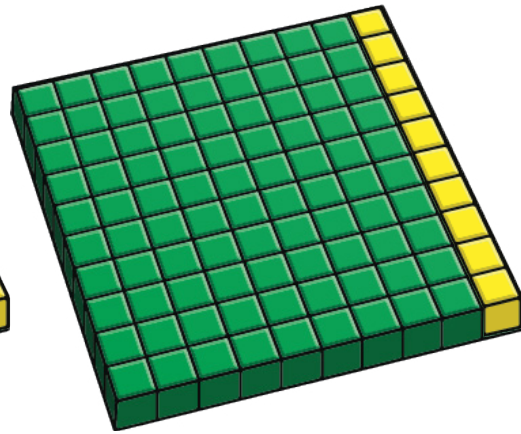
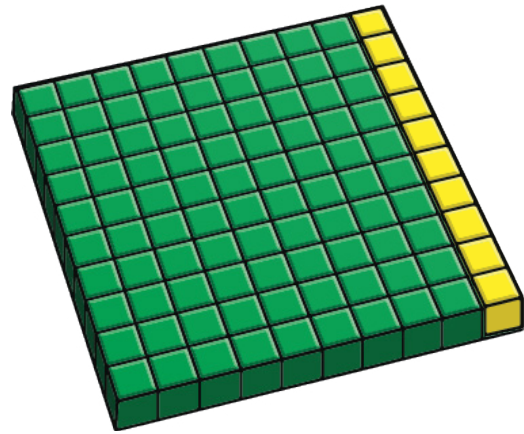
$\div 1000$

0.634



MD10b: Jump! (x10)

3/4 (Pictorial)



100 10 1

36

360

x10

